Crushed Rock Thermal Energy Storage & Nuclear Technology: Option Space & Economic Impacts

by

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B.S., Chemistry, United States Naval Academy, 2016 Submitted to the Institute for Data, Systems, and Society & the Department of Nuclear Science and Engineering in partial fulfillment of the requirements for the degrees

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Abstract

Increasing amounts of intermittent renewables have led to zero and negative priced electricity at times of peak wind and solar production. The volatility added to the grid by renewables and low prices at peak production create a demand for flexible energy supply and present an opportunity for energy arbitrage. Nuclear reactors in the United States are inflexible when compared to fossil generators, and batteries may store energy at peak renewable production, albeit at a high capital cost. Thermal energy storage coupled to nuclear reactors may both increase nuclear flexibility and capitalize on price volatility, benefitting the economics for the struggling nuclear industry. This research maps the option space for constructing a crushed rock thermal energy storage (TES) system coupled to a light water reactor and employs a modification of the GenX capacity expansion model to evaluate the economic. Historic demand and renewable resource availability from ERCOT were used to illustrate the benefit of crushed rock TES with an increasingly restrictive CO₂ emission constraint. Parametric variations were used to address uncertainty in performance estimates. Crushed rock TES was found to be beneficial under favorable conditions, reducing the average price of electricity from \$81/kWh (without TES) to \$73/kWh (with TES) at a system marginal cost of \$5/kWh-heat and emissions constraint of 100 g CO₂/kWh-electric, a nearly 10X reduction of current emissions. Unfavorable conditions resulted in a price reduction from \$81/kWh to \$78/kWh with the same cost estimates and carbon constraint. The investment cost of enabling the ability for nuclear generation to couple to crushed rock TES was also found to significantly affect the system's favorability and effect on electricity prices.

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Disclaimer: Nathaniel McLauchlan is an active duty Officer in the U.S. Navy. Any views, opinions, assumptions, or conclusions expressed in this work are those of the author and do not reflect the official policy or position of any agency of the U.S. government. As well, the author is responsible for any errors or deficiencies contained in this work.

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1. Introduction

1.1 Changing Energy Markets

Electricity markets have experienced significant changes in recent years due to both technological developments and a growing emphasis on mitigating anthropogenic climate change. These changes include an increasing shift towards renewable energy production in the forms of wind and solar generation, increased digitization of the energy grid, and a lessening reliance on fossil fuels. While such advancements are projected to limit future CO₂ emissions, they may also give rise to a fundamental change in the electricity grid that may require changes in energy policy.

Historically, energy production has centered on low-capital, high-fuel cost technologies; producing more energy simply required burning more carbon based fuels. In contrast, low carbon forms of energy production, wind, solar, and nuclear power, are high-capital, low-fuel cost technologies. In order for these technologies to remain as economically favorable over their lifetimes, they must operate at high capacity factors; operating nuclear reactors or wind farms at half capacity effectively doubles their lifetime cost. In addition to this phenomenon, renewables are intermittent, limiting their capability to match demand in real time. As a result, meeting energy demand with renewables absent energy storage technology, if possible, could require massive amounts of distributed renewable energy production.

The economic consequences of extensive renewable energy production without adequate storage technology are severe. The price of electricity is set through a bidding system, whereby the price reflects the lowest bid offered to meet energy demand at a certain time. Currently, renewable generation plants offer bids at or near zero cost reflecting their marginal costs of production, while fossil fuel burning plants effectively set the cost of electricity. Absent the burning of fossil fuels, the market is dominated by high capital, low fuel cost energy, and the price of electricity approaches zero or even negative costs in the presence of subsidies for renewables. This revenue collapse described extensively in MIT's *Future of Solar Energy* study eliminates the incentive for investment in renewable energy sources ("The Future of Solar Energy" 2015). Figure 1 below illustrates the effect that extensive investment in solar energy has had specifically on the price of energy in California, dropping to negative pricing during peak solar production. These negative prices reflect how much gas turbine operators are willing to pay the grid in order to remain

operating during peak solar production, enabling them to capitalize on high prices following the solar peak.

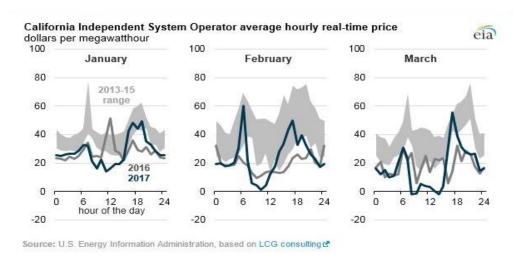


Figure 1 - Price Collapse at Times of High Solar Production in California ("California Solar Spike Leads to Negative CAISO Real-Time Prices in March" 2017)

In short, as fossil fuels are phased out in an effort to produce a greener energy grid, the price of energy will drop, removing incentives to invest in renewable energy. Implementing energy storage technology to stockpile energy at times of peak renewable production may provide a market for the excess energy, allowing the energy to be sold later at a non-zero price.

1.2 Energy Storage and Crushed Rock

Generally, energy storage technologies either store energy as work or heat. Work storage is favorable for technologies such as wind and solar photovoltaic (PV) generators whose primary output is electricity, while thermal storage is favorable for technologies such as nuclear reactors and concentrated solar thermal power systems which produce heat. The marginal cost of storing thermal energy is lower than the marginal cost of storing electric energy as work, due in large part to the complexity of the technology involved in storing energy as work, of which flywheels, pumped-hydro, and batteries are examples. In addition to avoiding revenue collapse, thermal energy storage when coupled to light water reactors (LWRs) has the added benefit of allowing nuclear reactors to provide essential reliability services (ESR) and run at maximum capacity, maintaining a low levelized cost of electricity (LCOE) for the high-capital-investment technology.

Various thermal storage technologies exist today, all with varying costs, energy capacities, and rate of energy charge and discharge. For instance, steam accumulators, are tanks of pressurized water that are heated by steam to their boiling point. When valves are opened, the water flashes to steam. Steam accumulators are used in some solar thermal plants for heat storage. This technology functions ideally as a buffer in steam plants, allowing for rapid charge and discharge cycles on the order of about a day's worth of energy, but would not be suitable for larger storage capacities given a high marginal cost of energy storage. (Charles Forsberg 2017) Geothermal heat storage systems, on the other hand, may provide seasonal energy storage dependent on its location. Thus, while daily and potentially seasonal variations in energy demand may be met through these technologies, a significant technology gap exists on the scale of multi-day to weekly storage.

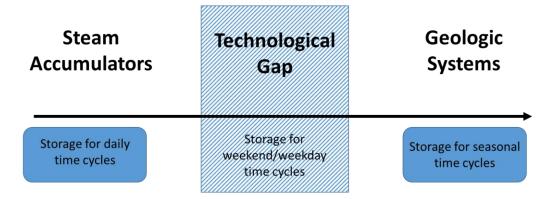


Figure 2 - Illustration of Technological Gap in Energy Storage

Crushed rock thermal energy storage (TES) may fill this technology gap, providing energy storage capacities of gigawatt-hours with faster response than geothermal heat storage systems and very limited geographic constraints.(C. W. . Forsberg, Curtis, and Stack 2017) The reasoning for the low marginal cost of energy storage with crushed rock thermal storage is intuitive: the primary material for the system is crushed rock, which is cheap, and the atmospheric operating conditions impose few expensive technological constraints. Figure 3 below illustrates the conceptual model of the crushed rock technology in the heating mode, whereby air is heated in a steam-air heat exchanger before being circulated through a large bed of crushed rock from top to bottom. Heat is recovered by reversing the flow.

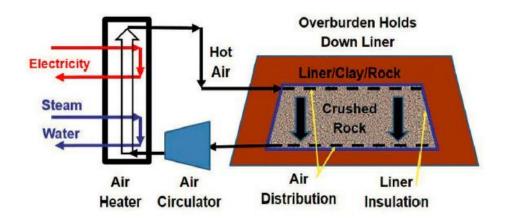


Figure 3 – Crushed Rock Thermal Energy Storage in Heating Mode

1.3 Structure of the Thesis

This thesis aims to answer the principal question of to what extent may crushed rock thermal energy storage provide flexibility in energy supply and mitigate revenue loss in a low-carbon energy grid primarily through the use of both engineering analysis and economic modeling. Chapter 2 consists of a literature review on drivers towards a lower carbon energy grid and existing energy storage technologies. Chapters 3 and 4 present the engineering analysis and economic models used to evaluate the potential option space for crushed rock TES, respectively. Chapter 5 summarizes the results, and Chapter 6 presents the conclusions.

2. Literature Review

2. 1 Evolving Electricity Markets

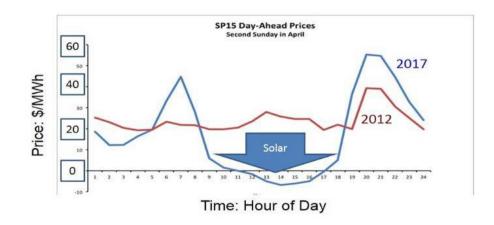
The turn of the century has seen a paradigmatic shift away from low capital, high fuel cost, on-demand energy policy towards one centered on greener technologies, increased digitization of the energy grid, and increased consumer awareness of energy supplies. Innovative renewable energy technologies and public awareness of anthropogenic climate change are upending the millennia old energy policy of simply burning more carbon based fuel to meet increased energy demand. As an increasingly larger share of the energy demand is met by intermittent renewable energy resources, the ability to provide adequate energy on demand is jeopardized. If present trends towards increased renewable energy penetration are to continue, the market may have to adapt with regards to monetizing storage and capacity, and energy sources such as nuclear energy may transition from their role as base-load energy providers to one of variable suppliers. Energy policy and legislation will certainly play significant roles in shaping the future of energy, hopefully for the better. This section outlines the structure of existing electricity markets followed by a brief account of drivers towards a low carbon energy grid, and a case for the future of nuclear energy.

2.1.1 Electricity, Capacity, and Auxiliary Services Markets

A structural understanding of energy economics is required before discussing the drivers towards a low carbon energy grid. In short, the electricity market consists of the energy market, the capacity market, and the auxiliary services market.

The energy market pays energy producers for the energy that is delivered to the grid, with the price set through a bidding system. That is, producers bid a day ahead for the price they are willing to sell energy for each hour. The highest price bid needed to meet demand for a given hour is then given to all producers who bid at or below that price. Nuclear and renewable energy producers typically bid at \$0, reflecting their low marginal costs. Thus, as long as intermittent renewables and nuclear do not fully meet electricity demand, the price is set by fossil fuels and all producers benefit. Absent the need for fossil fuels to meet demand, revenue drops substantially. Bidding at the margin in this way leads to revenue collapse with varying amount of clean energy penetration ranging from just 15% of total electricity demand met by solar to approximately 70% of electricity demand met by nuclear for certain markets (Charles Forsberg et al. 2017). This price

collapse is illustrated in the figures below for both solar energy in California and wind energy in Iowa (Charles Forsberg et al. 2017). Note the difference in time scales with the wind cycle spanning days and solar cycle spanning hours.



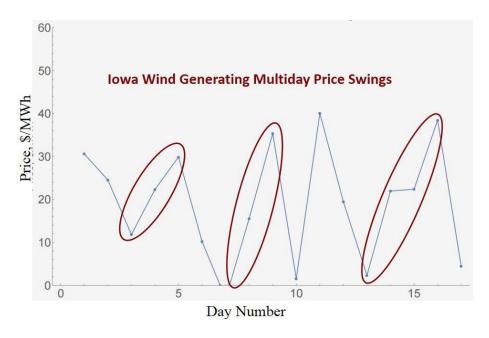


Figure 4 - Price Swings Due to Solar and Wind Energy

The capacity market is structured around assuring capacity to meet demand and avoid blackouts. This market is nearly negligible with adequate on-demand energy to meet demand. With heavy renewable penetration, however, capacity can either be assured by bulk storage capacity or the use of fossil plants designed to meet demand on the few hours a year of very high price spikes at times of low renewable production (Charles Forsberg et al. 2017). Alternatively, the electricity grid can make capacity payments (\$/kWe) to assure sufficient generating capacity to plants that

can assure supply when needed. Most electricity plants in the United States have chosen to provide capacity payments for assured electricity generation to avoid blackouts rather than see extreme electricity prices at times or higher risks of blackouts.

The auxiliary services market accounts for electricity grid services such as frequency control, maintaining spinning reserve, and black start. According to the 2017 DoE *Staff Report on Electricity Markets and Reliability*, essential reliability services (ERS) will become increasing important with increasing volatility in grid operations (U.S. Department of Energy 2017). Increasing amounts of variable renewable energy sources and distributed energy resources (DER) would increase volatility, and grid operators would face increasingly difficult challenges with respect to maintaining grid reliability and resilience. A few energy storage technologies may be able to provide these essential reliability services (ERS). However, the current revenue of these markets is only a few percent of the cost of electricity.

2.2 Drivers towards a low-carbon energy grid

2.2.1 Changing supply and demand side technologies

Both technologies producing and consuming energy have drastically progressed over the past few decades, both enabling more low-carbon energy production and increasing electric demand, particularly in the transportation sector. As shown in the 2016 MIT Energy Initiative's *Utility of the Future* report, the price of key technologies for the decarbonization of the energy grid have dropped drastically since 2008, allowing in part for 213 terawatt-hours of added global renewable energy resources in 2015 alone (Ignacio Perez-Arriaga and Christopher Knittel 2016).

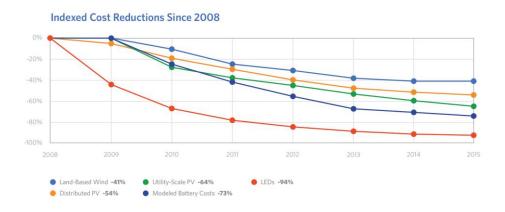


Figure 5 - Cost Declines in Key Technologies, 2008-2014; MIT Utility of the Future

In addition to decreasing renewable costs and increased renewable market penetration, the past few decades have seen changing energy demands, particularly in the transportation sector in the form of electric vehicles (EVs). EVs complicate energy market dynamics by functioning as both energy consumers and a distributed energy resource (Ignacio Perez-Arriaga and Christopher Knittel 2016). Increased electrification of the transport sector would complicate demand, likely increasing demand at night when EVs are charging and solar plants are not producing energy. A recent study by the California Energy Commission has shown that EV charging times are likely to peak with the rest of electricity demand in the early evening ("California Plug-In Electric Vehicle Infrastructure Projections: 2017-2025" 2018). Such a confluence presents a threat to grid stability and an opportunity for energy storage technologies to provide value. The figure below illustrates the projected load profile for EVs on a typical weekday in California.

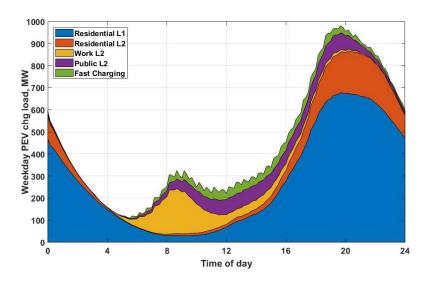


Figure 6 - Weekday Demand Load for EVs in CA

2.2.2 Policies Promoting a Low Carbon Energy Grid

While the prices of green technologies have decreased substantially, the auto-cannibalistic effect of renewable energy deployment, whereby the marginal cost of energy decreases with increasing renewable energy penetration, cheap fossil fuels, and the inertia of carbon based energy production all oppose the transition to a low carbon energy grid. Fortunately, international, national, and state-level policies exist which in part offset these hindrances to a low-carbon grid. Yet, many existing policies disproportionately favor renewable resources to other low carbon energy sources, such as nuclear energy. Legislation holistically promoting greener energy and storage technologies could accelerate the transition to a low carbon energy grid, while mitigating revenue collapse and intermittency concerns at the same time. A few of the existing policies supporting the transition to a low carbon energy grid are presented below.

The Renewable Electricity Production Tax Credit (PTC), administered by the U.S. Internal Revenue Service, is a federal policy which provides a tax credit to wind generators commencing construction by December 31, 2019 of \$0.015 per kWh in 1993 dollars. With adjustment for inflation and the 20% step-down as required by the Consolidated Appropriations Act, 2016, the 2017 calendar year credit was equivalent to \$0.019 per kWh (H.R. 2029 Consolidated Appropriations Act 2016; "Renewable Electricity Production Tax Credit (PTC) | Department of Energy" 2018). Policies such as the PTC certainly promote the expansion of wind energy, but do not benefit other clean sources of energy production, such as nuclear energy.

The Renewables Portfolio Standard (RPS) is an example of a state level policy. California's RPS has a target of 50% of retail sales derived from eligible renewable energy resources in 2030 and all subsequent years ("RPS Homepage" 2018). Nuclear energy is a low-carbon energy resource, but not a renewable energy resource, thus disqualifying it for the RPS.

The Paris Agreement or Paris Climate Accord is an example of an international agreement intent on curbing carbon emissions worldwide. The Agreement serves as a formal recognition of anthropogenic climate change and a document of good will towards limiting climate change with benchmark goals based on degrees of temperature elevation above pre-industrial levels ("The Paris Agreement - Main Page" 2018). Currently 173 countries have ratified the agreement, with the U.S. State Department having officially announced its withdrawal (*Reuters* 2017). According to the Agreement, however, the earliest effective withdrawal date for any country is November 4th, 2020

("The U.S. Won't Actually Leave the Paris Climate Deal Anytime Soon - The New York Times" 2017). Compared to the state and federal level policies in the United States, the Paris Agreement lacks enforcement measures or economic incentives, but rather relies on political capital between the countries. Countries that are party to the agreement are required to regularly report on their emissions and implemented strategies to further reduce carbon emissions, but policy enforcement and regulatory bodies are lacking.

2.3 Economic Prospects for Nuclear Energy Today

The largest barrier to nuclear energy other than fear of historic events and radiation is simply the economics of building new nuclear power plants. Nuclear power plants require huge capital costs that have only increased as a confluence of the intense regulatory state and increasing construction times for nuclear technology, specifically in the United States. Today, nuclear energy is not competitive with fossil fuels in the United States. Severe policies which monetize the negative externalities of CO₂ emissions, such as a carbon tax, may upend this paradigm. The levelized cost of electricity (LCOE) "represents the constant and theoretical cost of every kWh produced by an energy generation system along its useful life," and is often used to compare the costs of energy producing systems (Talavera et al. 2016). Through using the LCOE, energy systems with high initial capital investments, such as nuclear reactors, can be meaningfully compared to energy production systems with low initial capital requirements and high fuel costs, such as coal plants. Figure 1 below was taken from a report by the International Energy Agency (IEA), in which they demonstrated how economically competitive nuclear energy would be if the externality of CO₂ emissions was properly captured at \$30/ton of CO₂ (*Projected Costs of Generating Electricity*, 2015).

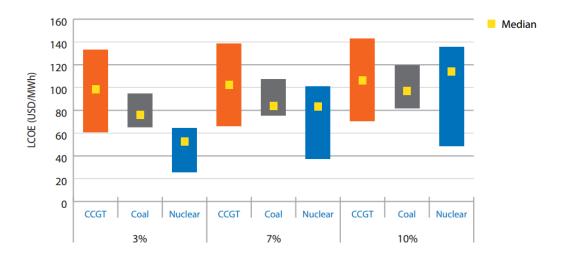


Figure 7: LCOE between Various Energy Technologies at Varying Discount Rates

The key assumption in the figure above, the economic capture of the negative externality of CO₂ emissions has yet to be realized, and even they may have a limited impact. A 2012 study estimates that a \$25 per ton of carbon dioxide tax in 2010 dollars would result in an LCOE for nuclear generation of 169% the cost of natural gas production instead of 202% without the carbon tax (Lucas W. Davis 2012). Unfortunately, even a carbon tax, which has been successfully implemented in Canada at \$10 per ton in 2018 and is planned to rise to \$50 per ton in 2022, may not make nuclear fission economically viable in the United States (Canada 2017).

Technological innovation, decreasing construction times, and emission constraining policies could make the economics favorable and provide routes for the expansion of nuclear generation. Emission caps in the interest of mitigating climate change could leave nuclear as one of a limited amount of technologies available to provide energy on demand. International cooperation and the support of developing countries, whose energy demands and thus emissions are expected to grow substantially, would likely be required in order for such policies to succeed. Garnering support across such a wide cross section of stakeholders would be difficult, and constraining policies would be economically inefficient. An alternative, technological innovation, may provide the answer for the future of nuclear.

Flexibility in power generation and the ability to provide ERS will become increasingly important as the penetration of renewable energy sources increases. Currently, nuclear reactors, especially LWRs in the United States, are ill suited for load following due to both their sunk capital

costs and the stresses induced by ramping reactor powers (U.S. Department of Energy 2017). At the same time, LWRs are the best understood nuclear technology in the United States, having benefited from decades of learning curves and a wealth of network information (Robin Cowan 1990). Coupling high-capital cost energy generation technologies, such as LWRs, to thermal energy storage (TES) could afford nuclear generation the flexibility in operation to provide ERS and become economically competitive in the presence of renewables. This would maximize electricity sales at times of highest prices (see Fig. 4).

2. 4 Energy Storage

2.4.1 Utility of Storage Technologies

Storage technologies have the ability to mitigate intermittency, match supply to demand, provide ERS, and smooth the energy output of nuclear generation in particular, which benefits from operating at its rated capacity. Recent advancements in both renewables and storage technologies have led to an increase in studies concerning the value of energy storage. A report from the Imperial College of London estimates, as expected, that value of energy storage technologies increases with increasing renewable energy penetration, potentially saving 10 billion pounds per year by 2050 in the United Kingdom (Goran Strbac et al. 2012). The report notes as well that the optimal composition of energy storage technologies differs according to regional availability of renewable energy resources, with bulk storage likely providing the most value in Scotland and distributed storage dominating the southern regions(Goran Strbac et al. 2012). Thus, for any given grid, determining the optimal energy storage portfolio and how to reward investors to appropriately reflect the value of storage are two of the most challenging questions which must be answered.

More recently, a group of researchers from the MIT Energy Initiative sought to answer the question of how different energy storage technologies should be compared (Braff, Mueller, and Trancik 2016). In short, the value of any energy storage system depends on their technical properties, such as their separate energy and power costs, intended applications, and regions and times at which they may operate. No single energy storage technology today is optimal across all dimensions, making any standalone comparison of energy storage systems both difficult and counterproductive. Thus, energy storage must be evaluated in concert with energy providers and consumers. Energy generators maximize efficiency by coupling to storage technologies based on

the form of energy stored, opting to store at an equal or higher energy quality. That is, photovoltaic solar (PV solar) and wind generation typically couple to electric storage systems such as batteries, while concentrated solar power (CSP) and nuclear generation could couple to thermal or electric storage systems.

In the specific context of nuclear technology, energy storage could allow for a low-carbon combination of technologies which could provide other essential reliability services. The figure below from the 2017 DoE *Staff Report on Electricity Markets and Reliability* illustrates the reliability attributes provided by each major energy producing technology as well as batteries and storage. Clearly, no single technology provides every attribute, with hydro generation, which is geographically constrained, coming the closest. However, a combination of nuclear generation and energy storage would at least partially provide each attribute from frequency response to fuel assurance and flexibility.

	(1	Essential Frequency, V	Reliability S oltage, Ram			Fuel As	surance		Flexibility		Other		
= Exhibits Attribute = Partially Exhibits Attribute	Frequency Response	Voltage Control		Ramp					Át.	Minutes			
= Does Not Exhibit Attribute	(Inertia & Primary)					x Output)			irts Per Da	ime < 30		rictions Hours)	actor
Resource Type			Regulation	Contingency Reserve	Load Following	Not Fuel Limited (> 72 hours at Eco. Max Output)	On-site Fuel Inventory	Cycle	Short Min. Run Time (< 2 hrs.)/ Multiple Starts Per Day	Startup/ Notification Time < 30 Minutes	Black Start Capable	No Environmental Restrictions (That Would Limit Run Hours)	Equivalent Availability Factor
Hydro													
Natural Gas - Combustion Turbine													
Oil -Steam									0		0		
Coal - Steam											0		
Natural Gas - Steam									0				
Oil/ Diesel - Combustion Turbine													
Nuclear									0		0		
Battery/ Storage						0	0						
Demand Response	0												
Solar													
Wind			0	0			0				0		

Figure 8 - Chart of Energy Technology Attributes (U.S. Department of Energy 2017)

2.4.2 Examples of Storage Technologies

A wealth of energy storage options exists today, and the valuation of each technology is complex. A few examples of energy storage technologies, both electric and thermal, are listed below to elucidate the distinguishing features which determine the range of storage utility. Further information on the thermal storage options listed below may be found in the 2017 Light Water Reactor Heat Storage for Peak Power and Increased Revenue Workshop Proceedings (Charles Forsberg et al. 2017).

Lead acid batteries currently dominate the distributed energy storage installations globally, but lithium-ion batteries are emerging as the favored form of electrical energy storage for electrical vehicles and other distributed applications coupled to renewable energy sources (Ignacio Perez-

Arriaga and Christopher Knittel 2016). The cost of lithium-ion battery packs without accounting for electronics has reportedly dropped 14 percent between 2007 and 2014, and has been projected to possibly fall to below \$100 per kilowatt-hour electric by 2022 (Ignacio Perez-Arriaga and Christopher Knittel 2016). While these price reductions represent a progression towards more affordable battery storage, they do not indicate that batteries storage will be cheaper than other forms of storage. Crushed rock TES, for example, has an estimated cost less than \$10 per kilowatt-hour of thermal energy (C. W. Forsberg, Curtis, and Stack 2017). The figure below illustrates the competitive cost of lithium-ion batteries relative to other battery technologies with a diesel generator for comparison (Ignacio Perez-Arriaga and Christopher Knittel 2016).

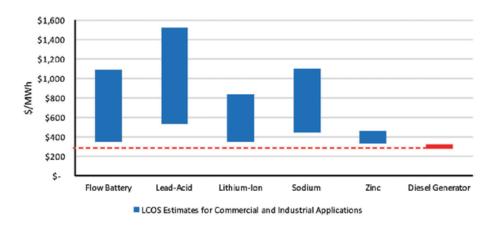


Figure 9 - LCOS for Various Technologies in Commercial and Industrial Application in \$/MWhe

One major advantage of lithium-ion batteries is its energy density relative to other energy storage systems. The current U.S. Advanced Battery Consortium's (USABC) target for electric vehicle battery pack density is 235 Wh/kg by 2020 (Li et al. 2017). Crushed rock TES may cost very little relative to lithium-ion batteries in regards to energy storage, but exhibits poor properties for energy storage in transportation. Lithium-ion batteries will very likely continue to grow in popularity, especially coupled to electric vehicles and distributed energy resources, such as roof mounted solar panels where minimizing weight or size is important, but may not be ideal for bulk energy storage, where these characteristics are not important.

Many TES options exist today, or are in development. Most of these technologies rely on storing energy and recovering energy by means of a phase change or through conduction and convection.

Steam accumulators store heat as high-temperature, high-pressure water, which is then flashed to steam to power a turbine generator. Steam accumulators are well-suited for CSP designs where steam is generated in pipes located at the foci of parabolic or Fresnel reflectors (Charles Forsberg et al. 2017). Due to the highly pressurized vessels, steam accumulators may exhibit higher marginal energy storage costs relative to atmospheric systems, and are ideal for rapidly supplying energy. Thus, steam accumulators could increase the short term flexibility of a nuclear plant, but would not be an ideal technology for balancing weekly energy demand. This technology is deployed at some concentrated thermal solar power plants.

Heat storage (oil, salt, etc.) in secondary low-pressure media provides a lower pressure alternative form of energy storage. This form of sensible heat storage involves heating a secondary fluid, and storing that fluid for later use. Many CSP plants use sensible heat storage in the form of molten salts, which can either be thermoclines or two-tank systems (Charles Forsberg et al. 2017). Sensible heat in solar power towers has been demonstrated up to the GWh scale. Westinghouse is developing a modular sensible heat TES system for nuclear reactors with each unit storing 1 MWh of electricity (Charles Forsberg et al. 2017). Westinghouse's design utilizes oil as a heat transfer fluid, which is used to heat concrete as a primary heat storage solid.

Cryogenic liquid air storage stores energy by liquefying air, and recovers energy through the evaporation and expansion of the fluid. If only warm cooling water from the nuclear plant or other low-temperature heat source is used, the estimated round-trip efficiency of a stand-alone system is around 60%, with potentially higher efficiency if steam is used to heat the air to higher temperatures (Charles Forsberg et al. 2017). In theory, cryogenic liquid air storage could couple to most reactor types.

Pressurized counter-current condensing-steam solid heat storage is similar to both steam accumulators and sensible heat storage, only heat is stored in a packed bed of solid pebbles under pressure before transferring the energy to water as the working fluid. The system is charged through the injection of steam, which condenses to water at high temperature, and discharged by filling the packed bed from the bottom with liquid water. While a pressurized, packed-bed TES

may face relatively high capital costs, it should theoretically exhibit a very high round-trip efficiency (Charles Forsberg et al. 2017).

Nuclear geothermal heat storage may provide enough energy storage to balance seasonal demand. In short, a nuclear geothermal heat storage system would consist of injecting hot water into a reservoir, heating the rock. Water can then be recirculated to recover the stored heat. While deep rock cannot be insulated, the storage size scales cubically, while the ambient losses to the surroundings scale squarely. Thus, as the scale increases, the ambient losses become decreasingly important. It is significant to note that geothermal heat storage cannot be built anywhere, but rather depends on site geology (Charles Forsberg et al. 2017). Thus, nuclear geothermal heat storage cannot balance energy demand everywhere.

Together these energy storage technologies present a wide option space for storing energy when coupled to a nuclear reactor, but leave a considerable technology gap in providing multi-day energy storage capacity. Geothermal energy storage may be able to meet seasonal and even weekly variations in demand, but requires suitable geological conditions.

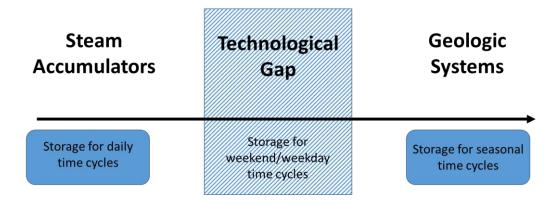


Figure 10 - Illustration of Technological Gap in Energy Storage

2.5 Crushed Rock Thermal Energy Storage

Crushed rock TES coupled to a nuclear reactor may fill this technology gap without geological constraints, allowing balancing of multi-day renewable energy cycles as seen with wind

generation in Iowa. Below is a summary of the technological concept followed by existing work related to crushed rock TES.

A hot rock energy storage system [McLauchlan, Appendix C; Forsberg, 2017a] is similar in concept to a packed bed energy storage system except that it operates at atmospheric pressure. A volume of crushed rock with air ducts at the top and bottom is created (Fig. 3.11). To charge the system, air is heated using a steam-to-air heat exchanger delivering heat from the reactor, then the air is circulated through the crushed rock heating the rock. To discharge the system, the airflow is reversed, and cold air is circulated through the crushed rock. The discharged hot air can be used to (1) produce steam for electricity or industry or (2) hot air for collocated industrial furnaces to reduce natural gas consumption.

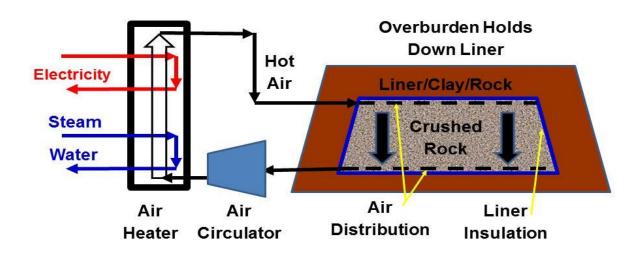


Figure 11 - Crushed Rock Thermal Energy Storage in Heating Mode

Heat storage systems are only charged at times of very low electricity prices. There is the option with this system to first heat the air with a steam-air heat exchanger and then further heat the air with electric resistance heating. LWR steam peak temperatures are near 300°C—well below the temperature limits of the crushed rock. Higher temperatures improve system efficiency and reduce costs. This can substantially boost rock temperatures and the efficiency of converting hot air back to electricity, and reduce capital costs. Near atmospheric operating conditions increase safety and reduce storage costs.

The economics may allow hourly, daily, and weekly storage. The longer storage times may be possible due to the very low incremental heat storage cost for crushed rock—far lower than any of the previous options that have been discussed. As such this technology can address the weekday weekend storage challenge where energy demand goes down on weekends but the production of wind, solar and nuclear does not if these facilities are operated at their full capacity. It is a storage technology that could potentially receive capacity payments for assured generation of electricity. With proper selection of rock for the expected peak temperatures, this storage system should be able to couple to most other reactors. The possible exception may be very high temperature reactors where finding suitable rock for such high temperatures may be difficult.

2.5.1 Related Work

Much of the engineering knowledge required to construct this large TES system has been developed through similar existing projects. A few companies and research groups have conducted work relating to Hot Rock TES to varying degrees, particularly in the development of thermal energy storage options for concentrated solar power.

Siemens Gamesa has begun a project to install hot rock heat storage in Germany to store wind energy. Unlike Hot Rock TES coupled to nuclear reactors, the Siemens project plans to use resistance heaters to heat airflow into an 800 cubic meter pile of crushed rock ("Siemens Gamesa Starts Construction Of Heat Rock-Fill Storage For Wind Energy" 2017). While this storage system is designed to provide approximately 30 MWh of electricity, Hot Rock TES coupled to nuclear reactors may provide tens of gigawatt-hours of electricity. The figure below presents a schematic design for the Siemens project.

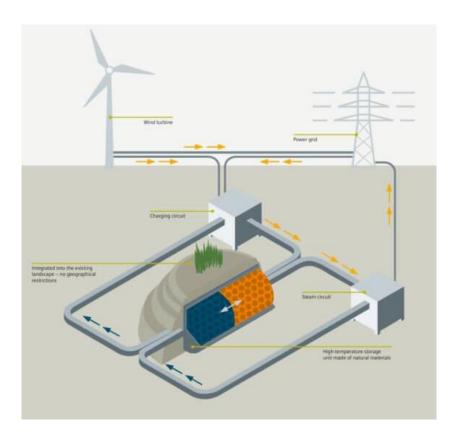


Figure 12 – Siemens Gamesa System ("Siemens Gamesa Starts Construction Of Heat Rock-Fill Storage For Wind Energy" 2017)

REDLEAF Resources Inc. is an oil shale company based in Utah, which is developing a large test bed for recovering fuel from a large pile of oil shale ("Red Leaf Resources, Inc. |" 2017). Crushed shale is heated with hot gases to decompose the solid kerogen in the shale to liquid and gaseous fuels. Oil shale volume shrinks as the kerogen decomposes. While this testbed may be representative of the potential size of the Hot Rock TES coupled to nuclear reactors, significant design differences limit the utility of REDLEAF's findings. The primary distinction comes in the form of thermal cycling and materials of interest. Whereas Hot Rock TES will cycle potentially hundreds of times a year, the REDLEAF oil shale capsule is designed for the sole purpose of recovering fuel and will be heated one time. Thus, the pile will shrink substantially in size throughout the thermal loading as solid kerogen is converted to oil, and the process will not bring light to the effects of repeated thermal loading on a Hot Rock TES using granite.

Crushed Rock Thermal Storage for Concentrated Solar Plants has gained traction as a field of study, namely in South Africa, Switzerland, Australia, and Morocco(Laubscher, von

Backstro'm, and Dinter 2017; Jemmal, Zari, and Maaroufi 2016; Barton 2013; Ha'nchen, Bru'ckner, and Steinfeld 2011). Unlike photovoltaic (PV) solar energy, concentrated solar power (CSP) produces power primarily in the form of heat by concentrating sunlight. Thus, thermal energy storage is attractive to CSP systems for many of the same reasons as with nuclear.

Researchers at the University of Stellenbosch and Solar Thermal Energy Research Group (STERG) in South Africa have gone as far as to construct an experimental testbed of a rock bed TES system with which to validate their smaller scale experimental correlations for temperature distributions and pressure drops throughout the system. An image of the prototype testbed is pictured below.



Figure 13 – STERG Group Experimental Rock Bed (Laubscher SolarPACES)

Much of the work conducted by the STERG and other universities in Europe and Africa has focused on developing models for the heat transfer within rock beds using air as the working fluid and evaluating rock types for system usability.

Barton, a researcher in Australia extensively simulated the heat transfer within a rock bed, accounting for the variation of fluid density with temperature and critically comparing potential engineering designs. Results suggested that selection of a heat exchange coefficient between air and rock particles, which depends on the mass-flow rate of air rather than the fluid density, simplifies calculations. From an efficiency standpoint, it is beneficial to charge the rock bed with

downward airflow and discharge with upwards flow, rather than charge and discharge both via upward flow(Barton 2013). This comparative advantage increases with increasing bed depth and decreasing mass flow rates. Barton has determined that the storage efficiency for the two-way system can be as high as 95% (Barton 2013).

Hanchen et al. conducted a similar heat transfer analysis for a rock bed using crushed steatite (a compact form of talc) and charging to temperatures up to 800 °C with daily 6-hour charge and 6-hour discharge cycles. The authors found that the system reached a cyclic steady state after about twenty daily cycles. From an engineering perspective, the highest overall efficiency was found with the smallest rock particles. As well, there seems to be a trade-off between the capacity factor and overall efficiency with high air mass-flow rates and low storage heights leading to the high capacity factors but decreased overall efficiencies (Ha"nchen, Bru"ckner, and Steinfeld 2011).

Researchers from the Moroccan Foundation for Advanced Science Innovation and Research (MAScIR), Mohammed V University, and the University of Stellenbosch have conducted research on various rock types for use in rock bed thermal energy storage. Jemmal et al. extensively studied the characteristics of two varieties of Moroccan gneiss rock up to temperatures as high as 1000 °C. The authors concluded that both types of the rock have good thermal stability up to 550 °C (Jemmal, Zari, and Maaroufi 2016). Allen et al. determined that, in general, non-foliated rock is preferable to foliated rock, and that dolerite withstood the effects of thermal cycling better than granite (Allen et al. 2014). As well, the authors determined that some types of sedimentary rock may be suitable for use in a rock bed thermal energy storage system (Allen et al. 2014).

Swiss Adiabatic Compressed Air Storage represents another field of study with many common concerns as for crushed rock TES. A pilot project in the Swiss Alps, contracted by the Swiss Federal Office of Energy, is assessing the suitability of caverns for compressed air storage with thermal energy storage to take advantage of renewable energy fueled energy arbitrage opportunities at low cost. One of the chief objectives of the pilot project is to understand the behavior of rock under cyclic charging and discharging operations as well as its suitability to house thermal energy storage (Giw Zanganeh 2016). The pilot plant currently exists, and the answers

that this project may provide are certainly relevant to crushed rock thermal energy storage. However, data gathered from the pilot plant are proprietary.

2.5.2 Considerations for Coupling Crushed Rock TES to Nuclear Reactors

Reactor Constraints

Nuclear reactors are a high capital, low variable cost energy producer. Operating reactors at the maximum operating capacity thus maximizes their lifetime value. That is, operating a reactor at half capacity effectively halves its lifetime value. Likewise, startup and shutdown processes increase operational costs, and should be avoided where possible. These constraints carry significant implications for coupling reactors to any form of thermal energy storage. Primarily, a minimum amount of steam must drive the primary steam turbine providing energy to the grid in order to avoid turbine startup and shutdown costs, as well as delays. This minimum value of steam to generation depends heavily on the specific reactor in question, but likely ranges from 30-70%, with new plants easily designed to operate at 30% of full load (Charles Forsberg et al. 2017). That is, the minimum value of steam generation is a product of design goals rather than technological constraints. Additionally, steam turbine efficiency decreases with decreasing loads. Thus, determining the optimal amount of steam flow to thermal energy storage systems will depend on the price of electricity, the efficiency of the turbine as a function of generation, and minimum generation constraints.

Reactor designs will also determine operating parameters such as the outlet temperature. Crushed rock TES may be suited for pressurized light water reactors (LWRs) as well as higher temperature reactors, as indicated by the range of thermal stability for rock types demonstrated by groups studying crushed rock TES for CSP. The rock type selected for use in crushed rock TES should depend on local availability to minimize costs and thermal stability for the expected temperature range and thermal cycling. Possible inlet temperatures to the crushed rock TES system could range from 300°C for LWRs to approximately 700°C for HGTRs and FHRs (Neil Todreas and Mujid Kazimi 2011).

Interface Constraints

When sending steam from the reactor to the hot rock, the steam is sent to a steam-air heat exchanger where the steam is condensed while air is heated. When going in the reverse direction there are two options. First, the steam-air heat exchanger may operate in reverse with the hot air producing excess steam from the reactor prior to the turbine hall. Second, a separate and customized steam air heat exchanger could be used. Design decisions will depend on priorities, namely capital costs and efficiencies. The first option incurs a lower capital cost than the second since the same equipment is used in both directions, but the second option allows for each exchanger to be optimized for its function. There would also be a significant size difference between the two exchangers, with the steam-air heat exchanger being roughly three times as large as the air-steam heat exchanger. This sizing difference would occur since large amounts of steam, perhaps as high as 70%, would be diverted to storage at times of low electricity prices, but peaking power from the thermal storage would be limited to 10-25% of the turbine capacity.

Energy Storage Independence and Integration

Energy storage systems may couple to nuclear reactors with varying degrees of independence. On one extreme, a storage system may couple to a completely independent turbine generator. Alternatively, the system could feed steam into the reactor turbine or feedwater heaters. The decision of whether to construct a separate turbine and generator or use existing machinery depends on existing equipment and desired electric output to the grid. Existing reactors may be able to increase the maximum electric output by 5-10% of the base-load power, whereas independent generators are not constrained to operate near base-load. Disadvantages to integrating storage systems with generators include limits to maximum peak power of approximately 10% above base-load power for existing turbines or 25% for new turbines, with an accompanying loss in turbine efficiency either at base-load or when peaking (Charles Forsberg et al. 2017). That is, a turbine optimized for output at 125% the rated capacity of a reactor will suffer an efficiency loss when operating at the reactor's rated capacity.

Diverting Steam for Process Heat

Precedent exists for the feasibility of splitting steam from nuclear production for multiple purposes. In countries such as Russia, Switzerland and Canada, nuclear plants have long provided variable electricity to the grid and steam to industry or district heating. This has not been the custom in the United States. In 2005, Fort Calhoun Nuclear Power Plant owners investigated

diverting steam to supply process heat to Cargill for processing corn. The project involved cost analyses, engineering assessments, and conversations with the Nuclear Regulatory Commission (NRC), which concluded the diversion would have no significant impact on safety(Charles Forsberg et al. 2017).

Estimating the Cost of Turbine Halls

Data also exists for estimating the cost of constructing oversized turbine halls. A report from Idaho National Labs indicates that the capital costs, including labor, of a complete turbine hall in terms of 2006 costs amounts to roughly \$500 per kilowatt of capacity ("Power Cycles for the Generation of Electricity from a Next Generation Nuclear Plant" 2010). Constructing a marginally larger turbine hall would likely cost hundreds of dollars per kilowatt of capacity, with most components remaining unchanged, save for the actual turbine and generator. The decision to feed heat from crushed rock TES to an existing turbine or feed water heater, expand an existing turbine, or construct a new generator entirely will depend on existing construction, the cost of turbine hall modifications, the cost of constructing a new turbine, and desired generator output.

3. Engineering Modeling and Option Space Estimations

Modeling technologies on the expected scale of the crushed rock TS system is crucial to demonstrating the viability of the concept prior to embarking on a costly engineering project. While economic models, which are further discussed in the following chapter, have the ability to illustrate economic competitiveness of various technologies, they rely heavily on technological parameters as well as capital and variable cost predictions, which are in turn validated through rigorous engineering analyses. Thus, the thermodynamic and economic models are closely linked in the evaluation of theoretical technologies and ultimately the decision whether or not to bring them to fruition. This chapter aims to estimate relevant parameters for the design of a crushed rock TES system, such as pressure drops and charging time, in order to outline the option space.

Prior to forming and presenting any model estimates, the driving motivations and potential biases must be considered. That is, models are by their very nature simplifications of complex, natural systems which are never truly closed, and model-makers have the ability to skew results through their choice of simplifications. Thus, as Naomi Oreskes, a Harvard Professor of the History of Science, has written: "models can be confirmed by the demonstration of agreement between observation and prediction, but confirmation is inherently partial" (Naomi Oreskes, Kristin Shrader-Frechette, and Kenneth Belitz 1994). For the purposes of this project, the thermodynamic model exists to provide insight to the technical limitations of the technology as well as order-of-magnitude cost estimates for various conditions. Simplifications made in the thermodynamic model presented in this thesis are recognized along with approximations as to how they may skew results. For example, neglecting conduction as a mode of heat transfer through the rock pile would result in an overestimate of the temperature of air extracted.

This chapter is organized into a sections on (1) the nomenclature used throughout the chapter; (2) general principles in modeling single-phase heat transfer in packed beds; (3) examples of experimentally vetted correlations for friction factors and heat transfer coefficients in irregular rock beds; (4) unique considerations for crushed rock TES borne out of system requirements; and (4) parametric estimates for a crushed rock TES system.

3. 1 Nomenclature

Table 1 below lists the nomenclature used throughout the chapter. The Biot number is a dimensionless quantity like the Reynolds and Prandtl numbers, but is less commonly used. In short, the Biot number represents the relative heat transfer resistances inside of and at the surface of a body. A Biot number much smaller than one allows for the assumption of uniform temperature within a body, whereas larger Biot numbers result in more complicated heat transfer problems.

Table 1 – Nomenclature for Engineering Estimates

Bi	Biot number	T	Air temperature [°C]
c_p	Air specific heat capacity [J/kg K]	t	Time [s]
CR	Particle specific heat capacity [J/kg K]	V_p	Volume of a particle, [m ³]
D	Equivalent particle diameter [m]	V_t	Total bed volume [m ³]
D_v	Volume equivalent Diameter [m]	V_S	Superficial flow speed [m/s]
h	Surface area heat transfer coefficient [W/m² K]	α	Void fraction
h_{v}	Volumetric heat transfer coefficient	μ	Air viscosity [kg/m s]
f	Friction factor	ρ	Air density [kg/m ³]
k	Air thermal conductivity [W/m K]	ρ_p	Particle density [kg/m ³]
k_p	Particle thermal conductivity [W/m K]	Δp	Pressure drop [Pa]
Н	Height of the rock pile [m]	Δt	Time interval [s]
m	Air mass flow rate [kg/s]	Δx	Segment length [m]
G	Air mass flux [kg/m ² s]	τ	Time constant [s]
NTU	Number of transfer units	\boldsymbol{A}	Surface area [m ²]
Nu	Nusselt Number		
Pr	Prandtl number		
Re	Reynolds number		

3.2 Modeling Single Phase Flow in Packed Beds

Heat transfer and pressure drops of single phase flow in packed beds are well-established fields of study. Most simply, both heat transfer and pressure drops depend on the particle material, heat transfer fluid, flow parameters, and geometry of the system, but to varying degrees. For the purposes of engineering design, pressure drops set limits on minimum pumping power required to force flow, while heat transfer determines the thermodynamic efficiency and temperature gradient in storing and removing heat from a packed bed. Both pumping power, a driving parameter for capital costs, and thermodynamic efficiencies, which strongly affect turbine efficiencies following output from the system, are primary concerns for the viability of crushed rock TES.

3.2.1 Pressure Drops

Pressure drops in packed beds are due to both frictional interactions between the heat transfer fluid and the change in gravitational potential energy as shown below in Eq. 1:

$$\Delta P_{Total} = \Delta P_{friction} + \Delta P_{gravity} + \Delta P_{form} + \Delta P_{acceleration}$$
 (1)

The form term accounts for pressure losses due to flow formation at both the inlet and the outlet. The acceleration term accounts for pressure variations due to a change fluid density that occur with changes in temperature. The gravitational term depends on the height of the system and the density of the fluid, and thus accounts for buoyancy effects due to the temperature gradient effects on the fluid density. The pressure loss due to friction depends highly on characteristics of the individual particles and the aggregate packed bed including the shape, roughness, and void fraction. Many correlations exist for predicting the pressure loss due to friction, with the most popular being the semi-empirical Ergun equation (Andrei Koekemoer and Adam Luckos 2015):

$$\frac{\Delta P_{fr}}{L} = 150 \frac{(1-\alpha)^2}{\alpha^2} \frac{\mu U}{(\varphi d_p)^2} + 1.75 \frac{(1-\alpha)}{\alpha^2} \frac{\rho_g U^2}{\varphi d_p}$$
 (2)

While the Ergun equation is a well-known model, it was derived from lab experiments utilizing relatively small, spherical particles, and any deviations from the controlled experimental environment result in modeling inaccuracies when translated to real-world systems. For example, beds of rough particles have been shown to produce higher void fractions than beds of smooth particles, and irregular particle size may result in a void fraction gradient with lower porosity towards the bottom of a packed bed, which would significantly increase the pressure drop due to

friction. Ultimately, correlations are only useful to the extent that they have been experimentally verified with the relevant conditions of interest.

3.2.2 Heat Transfer

In addition to the pressure drops, a temperature-time profile must be known in order to estimate the heat removal rate for a fluid at a given mass flow rate. This temperature profile may be estimated using an approximation for a one dimensional system, whereby temperature varies by axial segments using the Effectiveness-NTU method. It is important to note that this estimation accounts only for heat transfer via convection and neglects radiation and conduction entirely (K. G. Allen, T.W. von Backstrom, and D.G. Kroger 2015, 2015). Neglecting radiation and conduction is appropriate due to the relatively small temperature gradient, which is expected to remain below 400 °C. The fluid temperature at each segment can be expressed as:

$$T_{(i+1)} = T_{(i)} - (T_{(i)} - T_{p,i})(1 - e^{-NTU\left(\frac{\Delta x}{L}\right)})$$
(3)

With $T_{(i+1)}$ representing the air temperature at a segment i+1, and $T_{p,i}$ representing the rock temperature at segment i. The number of transfer units (NTU) depends on the volumetric heat transfer coefficient (h_v), mass flux (G), length of the particle bed, and specific heat capacity of the heat transfer fluid (c). The volumetric heat transfer coefficient in turn depends on heat transfer coefficient (h), surface area of particles (ΣA_i), void fraction, and total particle volume (ΣV_p) as follows:

$$h_{v} = h(1 - \alpha) \frac{\sum A_{i}}{\sum V_{p}} \tag{4}$$

The temperature of the rock at the next time interval is then:

$$T_{p,i}^{+} = \frac{T_{p,i} \left(1 - \frac{\Delta t L}{2\tau \Delta x} \beta\right) + T_{(i)} \left(\frac{\Delta t L}{\tau \Delta x} \beta\right)}{1 + \frac{\Delta t L}{2\tau \Delta x} \beta}$$
(5)

With:
$$\beta = 1 - e^{-NTU*\frac{x}{L}}$$
 and $\tau = \frac{m_p c_p}{mc}$ (6), (7)

Given the thermodynamic properties of the fluid and particle material, the void fraction in the particle bed and heat transfer coefficient must be established. The void fraction is a constant at a value between 0.3 and 0.45 for crushed rock, which depends on geometry of the rocks, and the heat transfer coefficient may be determined from an appropriate correlation for the Nusselt number.

3.3 Correlations for Modeling Flow in Irregular Rock Beds

3.3.1 Correlations for Friction Factors in Rock Beds

Absent the use of costly computational fluid dynamics (CFD) the construction of a thermodynamic model for crushed rock TES requires correlations validated with representative experimental testing. Fortunately, a research group from the University of Stellenbosch in South Africa has vetted various correlations for pressure drops and heat transfer in rock beds which are representative of crushed rock TES at a much smaller scale. Perhaps most importantly, the group determined that experimental results are required for predictions for pressure drop and the heat transfer coefficient to fall within 15% of the true value. Thus, the findings reported for the usability of various correlations should be considered heuristically as appropriate approximations at small scales may not apply at large scale.

Under isothermal conditions, a smooth sphere correlation valid from 10 < Re < 100000 consistently underestimates the friction factor for rock piles when compared to experimental results. Allen at al. have reported more accurate correlations for the friction factor of air at atmospheric pressure through crushed rock with both counter-current and cross-current flows respectively as (K. G. Allen, T.W. von Backstrom, and D.G. Kroger 2015, 2015):

$$f_{v} = \frac{\Delta p}{L(\frac{\rho v_{s}^{2}}{2})} \frac{\alpha^{3}}{(1-\alpha)} D_{v} = \frac{620}{Re_{v}} + \frac{13.7}{Re_{v}^{0.08}} \text{ and } f_{v} = \frac{\Delta p}{L(\frac{\rho v_{s}^{2}}{2})} \frac{\alpha^{3}}{(1-\alpha)} D_{v} = \frac{600}{Re_{v}} + \frac{12.3}{Re_{v}^{0.08}}$$
(8), (9)

With the effective volumetric diameter defined as:

$$D_{v} = \left(\frac{6}{\pi} \left[\frac{1}{n} \sum_{i=1}^{n} V_{pi} \right] \right)^{\frac{1}{3}} \tag{10}$$

And the Reynolds number defined as:

$$Re_{v} = \frac{\rho v_{s} D_{v}}{\mu(1-\alpha)} \tag{11}$$

The dependence on flow direction, either counter-current or cross-current, suggests that in addition to the materials used, the process of constructing a crushed rock TES system can significantly affect performance.

3.3.2 Correlations for Heat Transfer Coefficients in Rock Beds

The results also suggest that, unlike the frictional pressure drop, the heat transfer does not depend strongly on particle shape and flow direction, but rather almost entirely on the thermodynamic properties of the packing material used. Allen et al. used various correlations such as one provided by Wakao et al. to determine the Nusselt number, and thus the heat transfer coefficient for the flow, where:

$$Nu = \frac{hD}{k} = 2 + 1.1Re_p^{0.6}Pr^{1/3}$$
 and $Re_p = \frac{\rho v_s D}{u}$ (12), (13)

This correlation, which is appropriate for $15 < Re_p < 8500$ tracked experimental data well for a single charge with mass flux of $0.2 \text{ kg/m}^2\text{s}$ and temperatures circa 500 °C.

Barton and Hanchen et al. use the following correlation for the heat transfer coefficient in their calculations for air blown through a rock bed (Barton 2013; Ha¨nchen, Bru¨ckner, and Steinfeld 2011):

$$h = \frac{700}{6(1-\alpha)}G^{0.76}d^{0.24} \tag{14}$$

The utility of these correlations is limited to conditions under which they were experimentally validated.

3.4 Specific Considerations for Crushed Rock TES

Of course, the small rock bed used to experimentally validate these correlations is not perfectly representative of a 30-meter-tall crushed rock pile running multiple cycles with significant latent periods between charging and discharging. The isothermal conditions used in determining the correlations presented do not account for the crushed rock TES system's expected buoyancy effect due to the temperature gradient, and as a result underestimate the total pressure drop. As well, the friction factor was reported to increase over the course of multiple cycles and remain constant thereafter. This change in friction factor was likely due to the movement of small particles within the pile, effectively altering the void fraction throughout the pile.

Some deviations from the small scale experimentally determined correlations may, however, be anticipated and engineered against. For instance, Zanganeh et al. reported that the

axial void fraction distribution of their packed bed system decreased monotonically with increasing packed bed height to an asymptotic value of 0.325 (G. Zanganeh and et al. 2012). This variation in void fraction was likely due to both the total weight of the system bearing down on itself and the random dispersion of particle sizes which filled lower voids throughout the course of cycles. For the case of crushed rock TES on a large scale, a dead zone may be engineered to allow dust and particulate to accumulate at the bottom of the system below the outlet air ducts so that air flow is not unnecessarily impeded. For the purposes of this thesis, a conservative value of 0.3 is assumed for the void fraction.

Additionally, the anticipated time scale of the crushed rock TES system may affect primary assumptions for the heat transfer mechanisms. In the case of the Stellenbosch rock bed analyzed by Allen at al., conduction through the system was neglected due to the low calculated Biot number (<0.1) and short time scale of charging and discharging during which forced convection surely dominated. Instead of discharging immediately, crushed rock TES will not always charge from a completely discharged state, and may idle for many hours before discharging heat to industry or a turbine, which may provide ample time for the entire system to thermalize. Neglecting thermal losses at the wall, this process would not decrease the total amount of energy stored, but would reduce the gradient and ultimately the maximum outlet temperature during discharge, which is directly related to the turbine efficiency.

3.5 Parametric Estimates for Crushed Rock TES Option Space

3.5.1 Thermal Losses at the Walls

If the efficiency losses at the walls are not neglected, then the time scale of energy storage becomes increasingly important as energy is lost over time. Fortunately, the large scale of the system opposes this effect as the surface area (heat loss) increases as the square of the dimensions whereas the volume (storage capacity) increase as the cube of the dimensions. Ergo, the larger the system is, the smaller the portion of energy lost to the surroundings will be for a given time period. The Swiss Federal Office of Energy (SFOE) published a report in which fiberglass, concrete, and proprietary material were used to insulate rock up to 550 °C (Giw Zanganeh 2016).

Additionally, thermal losses to ambient conditions may be estimated for a system at a given temperature with a given amount of insulation. Figure 1 below illustrates an estimate for the effect of insulation thickness on the percentage of energy lost to ambient surroundings after one day for an approximately 10 GWh crushed rock TES system with the geometry of a 20-meter cube and an internal to external temperature difference of 300 °C. Fiberglass insulation is assumed with a thermal conductivity of 0.04 W/m K ("Thermal Conductivity of Common Materials and Gases" 2003).

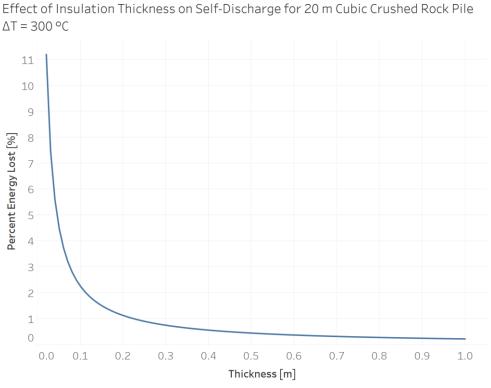


Figure 14 - Effect of Insulation Thickness on Ambient Energy Losses over 24 Hours for Crushed

Rock TES System

This estimation was calculated using equations from The Engineering ToolBox website for calculating heat loss from buildings ("Heat Loss from Buildings" 2003). Heat loss caused by ventilation and infiltration were neglected. Heat loss through the roof and walls were calculated respectively as:

$$H = 1.15 * A * U * (T_i - T_o) \text{ and } H = A * U * (T_i - T_o)$$
 (15), (16)

The factor of 1.15 for the losses from the roof estimates radiative losses to space. The overall heat transmission coefficient (U) was calculated as:

$$U = \frac{K_i}{X_i} \tag{17}$$

Where K_i and X_i are the thermal conductivity and thickness of fiberglass, respectively.

3.5.2 Pressure Drop

The pressure drop through one meter of crushed rock was estimated using a conservative void fraction of 0.3 and the experimental correlation for friction factor, eq. 9 given by Allen et al. for crushed rock with cross-current flow. The distinction between cross-current and countercurrent flow depends on the particle alignment relative to the flow direction of a fluid. Allen et al. found that packing particles in a co-counter-current manner results in higher friction factors than packing particles perpendicularly to the flow (K. G. Allen, T.W. von Backstrom, and D.G. Kroger 2015). As expected, the pressure drop increases exponentially with both increasing superficial flow velocity and decreasing rock diameter. These effects are shown in the figure below.

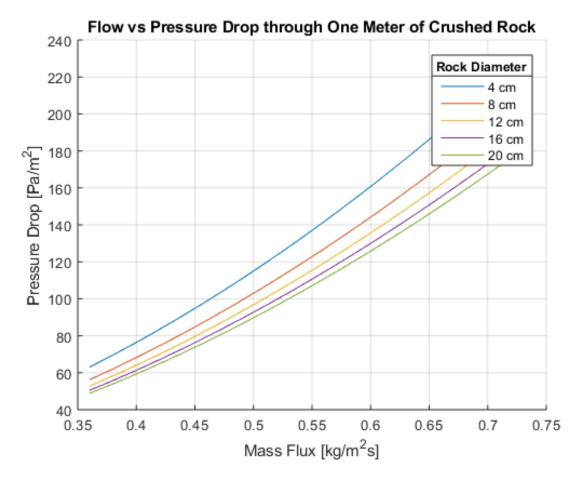


Figure 15 - Pressure Drops as a Function of Mass Flux and Rock Diameter

The total pressure drop for a column of crushed rock can be estimated as the product of the height of the column and the pressure drop per meter of crushed rock. Pressure drops due to gravity are approximately 10 Pa for a meter of crushed rock, and are thus insignificant when compared to the frictional pressure drop.

3.5.3 Temperature Distribution and Charging Time

The temperature distribution and charging time for the system is calculated as a simplified, onedimensional heat transfer problem with the assumptions that (1) air is an ideal gas with constant specific heat capacities; (2) the thermal mass of the rocks is much greater than the thermal mass of the flowing air, such that the temperature front advances sharply. That is, the change in temperature of the rock is equal to the change in temperature of the air at the heat transfer front; (3) the mass flux through the rock bed is constant; (4) the void fraction through the rock pile is constant; (5) the rock bed is comprised of identical spherical particles; (6) there are no storage system surface heat transfer losses; (7) conduction through the rocks is neglected; (8) radiation is neglected. Assumption (2) simplifies the calculation for the speed at which the heat transfer front moves through the packed bed, but breaks down as the mass flux through the system is increased.

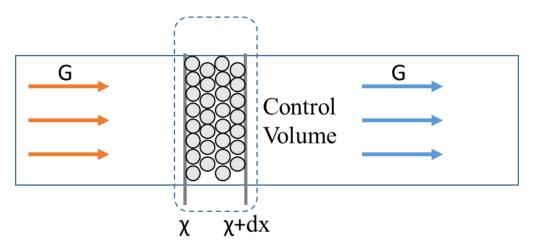


Figure 16 - Illustration of Heat Transfer Simplification

First, the conservation of momentum for the control volume holds that the mass flux through the system remains constant.

$$\frac{dm}{dt} = 0 \tag{18}$$

The conservation of energy equation for the control volume is:

$$\frac{\partial E_{CV}}{\partial t} = 0 = Q + mh_x - mh_{x+dx} \tag{19}$$

The conservation of energy equation for the rocks is:

$$\frac{\partial E}{\partial t_R} = \frac{d}{dt} \left[\rho_p A dx c_R T_R \right] = -q' dx \tag{20}$$

The conservation of energy for the air is:

$$\frac{\partial E}{\partial t_g} = -GAc_p dT_g = GAc_p dT_R = q'dx \tag{21}$$

Combining equations (20) and (21) and rearranging:

$$\frac{dT_R}{dt} + \frac{Gc_p}{\rho_p c_R} \frac{dT_R}{dx} = 0 \tag{22}$$

The general solution for this partial differential equation is a one-dimensional wave with the form:

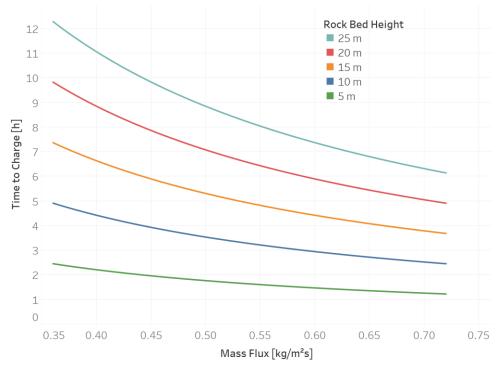
$$u(x,t) = F(x-ct) + G(x+ct)$$
(23)

Here, the coefficient $\frac{Gc_p}{\rho_p c_R}$ represents the speed at which the temperature wave flows through the rock bed, and the solutions to equation (22) are:

$$T_R(x,t) = F\left(x - \frac{Gc_p}{\rho_p c_R}t\right) \tag{24}$$

Thus, under the given assumptions, the charging and discharging rates of the system depend on the mass flux of the air, the relative specific heat capacities and the density of the rocks. The figure below shows the calculated time to charge a crushed rock thermal energy storage system with varying heights and mass fluxes of the air. The density of granite (2750 kg/m³) and specific heat capacities of granite (0.790 kJ/kg K) and air (1.005 kJ/kg K) were taken from the engineering toolbox website ("Densities of Solids" 2009; "Specific Heat of Common Substances" 2003).

Time to Charge as a Function of Mass Flux





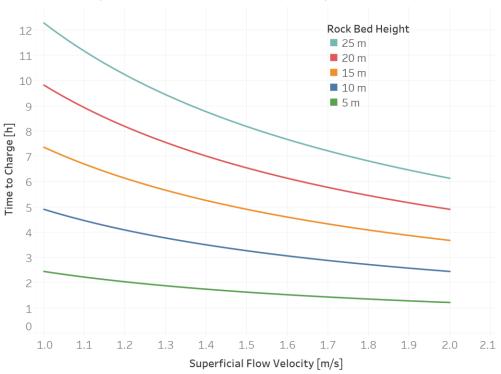


Figure 17 - Time to Fully Charge as a Function of Mass Flux, Air Velocity, and Rock Bed Height

3.5.4 Sizing Energy Storage

The maximum storage capacity of the system can be modeled as the maximum internal energy of the rocks at a full charge which can be transferred to the discharging air. That is:

$$E_{internal} = HA\rho_p(1-\alpha)C_R(T_{max} - T_{min})$$
(25)

It is important to select proper dimmensions, however, since there are tradeoffs. For a given storage capacity, shorter systems require more land. Conversely, taller systems result in higher pressure drops and thus require greater pump work to fully charge the system in a given time. The figure below illustrates this phenomenon. The pump work required is $W_p = 2v\Delta Pt$, where pressure drop is calculated with Ergun's equation (eq. 18 in Barton), the time to charge is calculated as in the previous section, and the factor of 2 reflects the need to pump air into and out of the system. The energy stored is calculated as $E_{stored} = C_a G \Delta T t \eta$, and the ratio of pump work to energy stored is W_p/E_{stored} . The code used to produce the following figures was validated against values provided in Barton (Barton 2013). A 50% heat to power efficiency is used here, which reflects the efficiency in converting heat to electricity. That is, 2 kWh of heat energy are equivalent to 1 kWh of electricity with a 50% heat to power efficiency. The heat to power efficiency, particle diameter, and temperature difference all have significant impacts on the calculated results, with high values for all parameters leading to the most ostensibly favorable results. However, heat to power efficiency is limited thermodynamically, large particle diameters lead to relatively diffuse temperature fronts, and inlet and outlet temperature differences are determined by reactor design and ambient external temperatures.

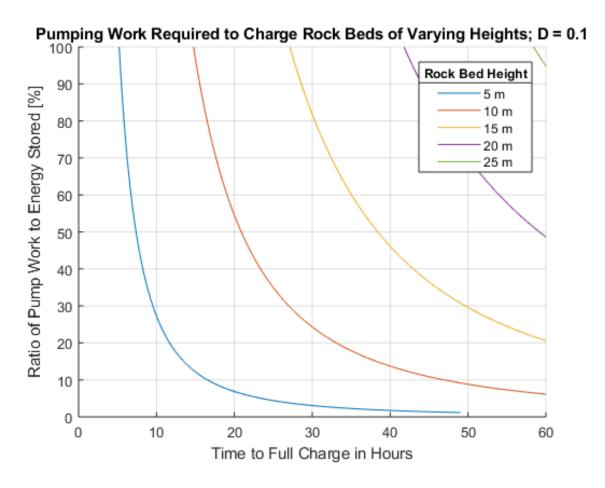


Figure 18 - Pump Work Ratio for Varying Rock Bed Heights and Charging Times D = 0.1 m

Intuitively, the amount of pump work required to fully charge the heat storage increases as the rock bed height and flow velocity, which is related to the time to full charge, increases. Increasing the particle size significantly reduces the pump work required, but results in a less efficient heat transfer, which is not observed here. The figure below illustrates the effect of doubling the particle diameter to 0.2 m. Both figures use the same scale for comparison.

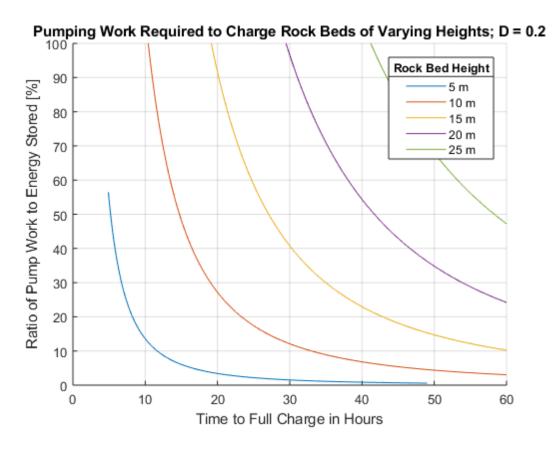
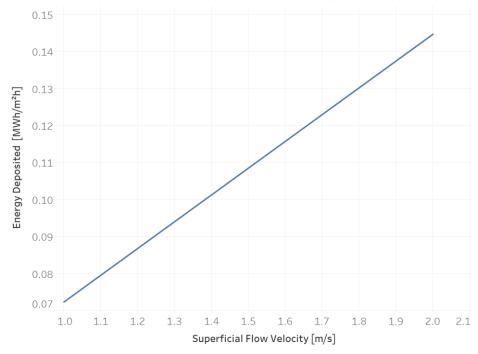


Figure 19 - Pump Work Ratio for Varying Rock Bed Heights and Charging Times D = 0.2 m

The rate of heat deposition is another important parameter for sizing the energy storage system. In short, the rate of heat deposition determines how quickly energy can be deposited and recovered from the energy storage. The graphs below illustrate the effect of flow velocity and mass flux on the rate of heat deposition as a function of mass flux and flow velocity. The rate of heat deposition from the air is calculated as $P_{deposited} = C_a G \Delta T$, with a temperature difference, ΔT , of 200 °C. The void fraction of the rock pile does not affect the rate of heat deposition, but rather determines the height of rock required to hold the deposited heat.





Heat Deposition as a Function of Mass Flux

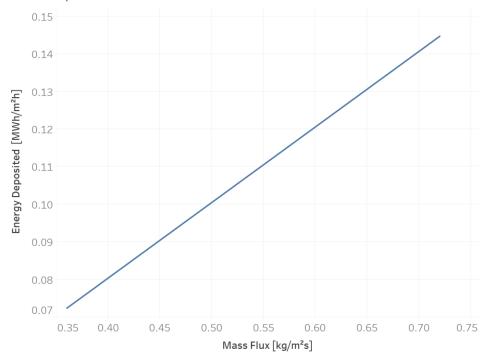
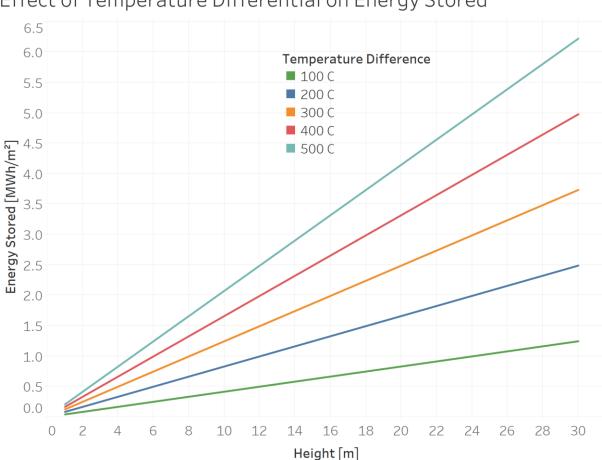


Figure 20 - Heat Deposition as Functions of Mass Flux and Flow Velocity

The amount of energy stored scales linearly with the temperature difference. The figure below illustrates the effect of the temperature difference on the total storage capacity. The amount of energy stored is calculated as $E_{stored} = (1 - \alpha)\rho_p c_R H \Delta T$, with a void fraction of 0.3.



Effect of Temperature Differential on Energy Stored

Figure 21 - Effect of Temperature Differential on Energy Stored

3.5.5 Estimating the Temperature Front

The interface between the hot and cold regions becomes more diffuse as particle size increases. This result is intuitive, since the efficiency of the heat transfer increases with increasing surface area, which increases as particle diameter is reduced. Barton calculated the spread of the hot-cold interface in a 1.6-meter-tall bed of steatite with an air mass-flow rate of 0.08 kg/(m²s) and varying particle sizes. Particle diameters of 2 mm to 10 mm corresponded to a transition region 0.5 to 1 meter in length (Barton 2013). Accurate estimates of the temperature front for a larger

system with two-way flow and multiple cycles requires experimental validation, but trends are predictable. Increasing particle size and flow rates, which reduce heat transfer efficiency, increase the length of the temperature front.

3.6 Future Work for Engineering Analysis

Further work is required for both accurate modeling of the crushed rock thermal energy storage system and the tradeoffs produced by design decisions. In particular, modeling pressure drops and heat transfer through the rock bed require experimental validation. Relaxing assumption (2) in the heat transfer analysis results in a more complex calculation for the heat transfer between the air and rocks with the governing equation:

$$\frac{\partial^2 T_R}{\partial t \partial x} + \frac{h}{\rho_p A c_R} \frac{\partial T_R}{\partial x} + \frac{h}{m c_p} \frac{\partial T_R}{\partial t} = 0$$
 (26)

Solving this partial differential equation requires that the heat transfer coefficient, h, is known. Correlations for determining the heat transfer coefficient are limited insofar as they are validated experimentally in representative systems. The crushed rock thermal energy storage system proposed in this thesis is an order of magnitude larger than the rock piles used to validate the heat transfer correlations listed in this chapter. Future work on this subject would include determining appropriate heat transfer correlations for rock beds which are tens of meters tall and subsequently modeling the behavior of the heat transfer front. The total length of the temperature gradient during charging and discharging will determine the optimal height of a crushed rock TES system for a given amount of energy storage capacity.

The tradeoffs for design decisions must be better understood as well. Building a taller system for a given capacity requires less land, but significantly increases the pump work required to charge and discharge the system. As well, increasing the particle diameter of the rocks would decrease the pump work required, but at the expense of heat transfer efficiency. In addition to these generally well understood phenomena, there are other complications that may arise with a large scale rock bed. For instance, the void fraction may vary significantly for tall rock beds due to settling dust and heavy overburden. Implementing a dead zone below the lower air ducts may correct for this effect, but experimental validation is required to determine how signification the variation may be. In general, the body of knowledge behind irregular rock beds informs general

trends and relationships between design choices, but these trends may not scale linearly, requiring experimental validation on large scale. Because heat transfer and pressure drop are in one direction, experiments must be the height of the storage system, but the cross sections can be small but large relative to the crushed rock diameter to avoid wall effects.

Calculations used to produce the figures throughout this chapter are detailed in Appendix A.

4. Economic Modeling

4.1 Common Electricity Market Models

Grid-level electricity generation relies on a complex mix of generating technologies, each with varying operational capabilities and associated costs. Since no single technology is purely dominant over others, the optimal energy portfolio contains varying levels of production from a mix of generation sources. The optimal mixture is not easily intuited, which has resulted in the use of extensive economic modeling for informing both grid operations (production cost modeling) and investment decisions (capacity expansion modeling).

Production Cost Modeling focuses on short term decision making on the order of hours or minutes. These models can be optimized to either maximize profits or determine the least cost means of meeting demand in a given region with a given set of generators. While production cost models produce valuable information for grid operators, they provide poor insight for investment decisions and do not address all aspects of reliability (Erin Boyd 2016). For this reason, production cost modeling is not ideal for the techno-economic assessment of novel technologies.

Capacity Expansion Modeling, as the name suggests, focuses on investment decisions for expanding capacity through the investment of new generators. Inputs to a typical capacity expansion model include estimates for future demand, the prices and operational parameters of generation, and policies such as expected subsidies and taxes (Erin Boyd 2016). Capacity expansion models are ideal for techno-economic assessment of novel technologies due to their longer time horizons. However, many existing models are not able to accurately model the effects of intermittency from renewable energy generation due to poor temporal resolution.

4.2 GenX Formulation

The increasing complexity of the power sector requires higher resolution decision making. Until recently, however, capacity expansion models were not capable of providing enough detailed insight for decision making in the face of a growing renewable sector, increased electrification of transportation, and massive deployment of distributed energy resources. Researchers at MIT formulated GenX as a tool to overcome previous limitations, allowing for more detailed, modular

results (Jesse D. Jenkins and Nestor A. Sepulveda 2017). GenX is "a highly configurable electricity resource capacity expansion model." Using constrained optimization, the model "determines the mix of electricity generation, storage, and demand-side resource investments and operational decisions to meet electricity demand in a future planning year at lowest cost subject to a variety of power system operational constraints and specified policy constraints." A basic electricity market considering generation from renewable and thermal generators and demand balanced by connected zones, demand side management, and storage technologies forms the basis of the formulation for GenX. Figure 22 below provides a graphical illustration of this system.

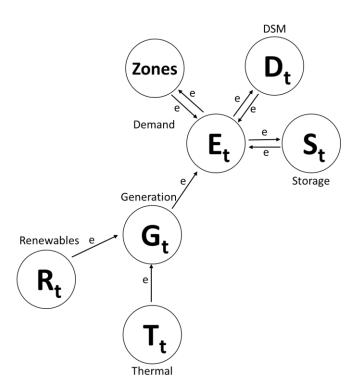


Figure 22 - System Level Illustration of Electricity Market without TES

Unlike most capacity expansion models, GenX has the capability to perform simultaneous co-optimization along seven decision layers, including capacity expansion planning, hourly dispatch of resources, unit commitment decisions, commitment of generation, transmission power flows, distributed network power flows, and interactions between electricity and heat markets (Jesse D. Jenkins and Nestor A. Sepulveda 2017). This dimensional modularity allows users to optimize the resolution of the model results along dimensions of interest while simplifying the others. With regards to the techno-economic assessment of crushed rock thermal energy storage, this flexibility allows for a high temporal resolution analysis of generation expansion and

interactions between the heat and electricity market without being too computationally cumbersome.

4.3 Modeling Crushed Rock Heat Storage with GenX

4.3.1 System-Level Model

In addition to determining optimal energy portfolios of existing technologies, GenX can function as a tool for the techno-economic assessment of novel technologies. This approach was employed to evaluate the impact of heat storage technologies, namely FIRES (Firebrick Resistance-heated Energy Storage) coupled to a Nuclear Air-Bryton Cycle, on the cost of decarbonization (Jenkins and Sepulveda, 2017). Figure 23 below illustrates how FIRES would alter the base scenario for GenX, allowing excess electricity to heat FIRES to either provide heat as a topping cycle for a fluoride salt-cooled high-temperature reactor (FHR) or export heat to the local heat market.

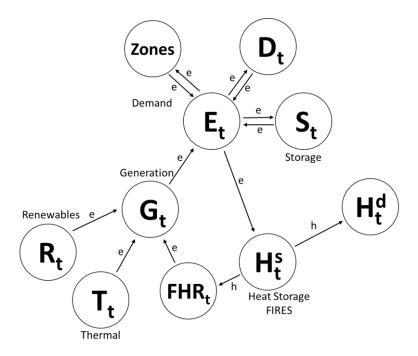


Figure 23 - System Level Illustration of Electricity Market With FIRES

A similar graphic can illustrate the theoretical relationship between crushed rock TES and the existing market. Unlike FIRES, which are heated using electricity and resistance heaters, crushed rock TES would charge using heat produced from a LWR at times of excess renewable production in order for the LWR to capitalize when renewable production is low. As with FIRES, crushed rock TES could provide heat to a local heat market, reducing a need for fossil fuels in manufacturing and other heat-intensive industries. Unlike FIRES with an FHR, the charging phase of the TES limits the coupled reactor's maximum energy output. Figure 24 illustrates the conceptual relationship of crushed rock TES to the rest of the system.

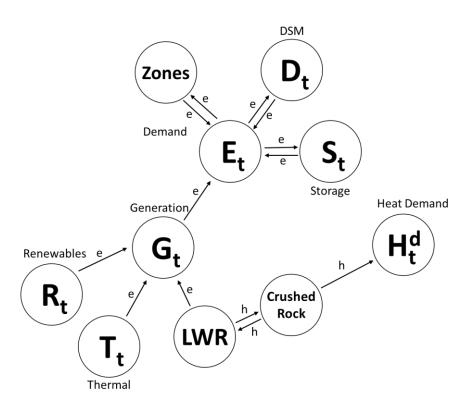


Figure 24 - System Level Illustration with Crushed Rock TES

4.3.2 LWR Base Case Formulation

The interaction between a crushed rock TES and a LWR carries significant implications for adapting GenX to model crushed rock TES. The base-case constraints for modeling a LWR are detailed below, followed by modified constraints for incorporating crushed rock TES.

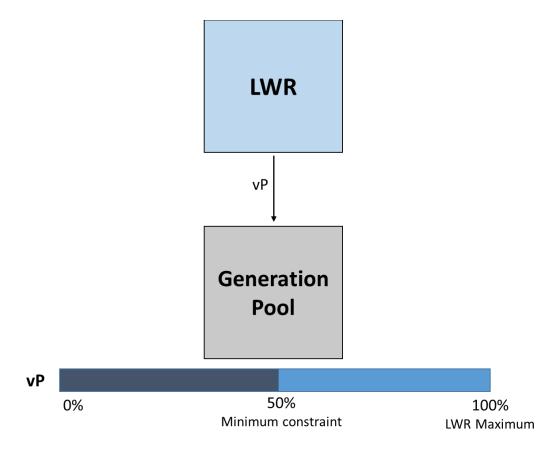


Figure 25 - LWR Base Case Interaction with the Generation Pool

Table 2 - Parameters for LWR Base Case Formulation

Parameter Notation	Description
$ ho_{LWR}^{min}$	Minimum stable power output per LWR [%]
$ ho_{\scriptscriptstyle LWR}^{ramp-up}$	Maximum amount of capacity the power output may increase in a time period $t[\%]$
$ ho_{LWR}^{ramp-down}$	Maximum amount of capacity the power output may decrease in a time period $t[\%]$
C_{LWR}^{max}	Maximum capacity for an LWR

Table 3 - Variables for LWR Base Case Scenario

Variable Notation	Description	
vC	Generator Capacity[MW _e]	
vP	Generator Power [MW _e]	

Table 4 - Constraints for LWR Base Case Scenario

Constraint	Description
$vP \leq vC$	The power output must be less than the maximum capacity
$vP \geq vC * \rho_{LWR}^{min}$	The power output at any time must exceed the minimum power
$vC \leq C_{LWR}^{max}$	The model can only choose to install capacity up to a maximum value
$vP_t - vP_{t-1} \le vC * \rho_{LWR}^{ramp - up}$	Changes in power output are limited by the ramp-up rate
$vP_{t-1} - vP_t \le vC * \rho_{LWR}^{ramp - down}$	Changes in power output are limited by the ramp-down rate

4.3.3 LWR with Crushed Rock Thermal Storage Formulation

Incorporating thermal energy storage can allow a LWR to provide peaking power at the cost of an efficiency loss at the heat exchangers to and from the storage unit. The maximum charge and discharge rates of the storage unit would impose constraints as well.

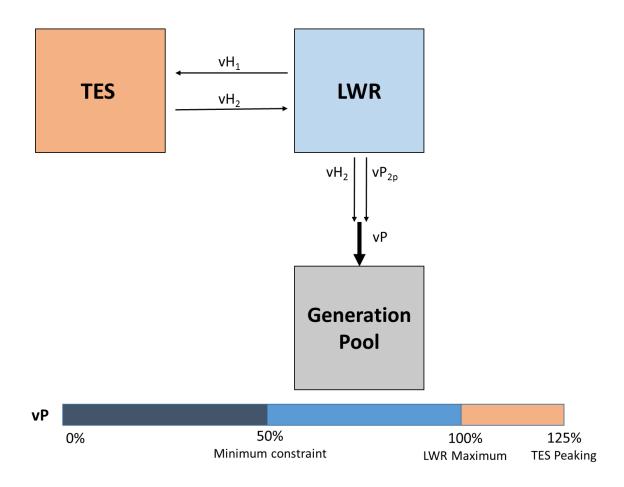


Figure 26 - LWR with TES Interaction with the Generation Pool

Table 5 - Parameters for LWR with Crushed Rock TES

Parameter Notation	Description
$ ho_{LWR}^{min}$	Minimum stable power output from the LWR [%]
$ ho_{Turb}^{min}$	Minimum stable power output from the turbine hall [%]
$ ho_{\scriptscriptstyle LWR}^{ramp-up}$	Maximum amount of capacity the power output from the LWR may increase in a time period t [%]
$ ho_{LWR}^{ramp-down}$	Maximum amount of capacity the power output from the LWR may decrease in a time period t [%]
η_{vH1}	TES charging efficiency [%]
η_{vH2}	TES discharging efficiency [%]
δ^{heat}	Peak to base generation ratio for LWR [%]
γ	TES self-discharge [%/t]
α	Electricity to heat conversion [MW _h /MW _e]

Table 6 - Variables for LWR with Crushed Rock TES

Variable Notation	Description				
vCap	Rated capacity of an LWR [MWe]				
νP	Total power to the generation pool from TES and the LWR [MWe] $$				
vP_{2p}	Power from the LWR to the grid [MW _e]				
vS	Thermal energy storage capacity [MWh _h]				
vL	Level of TES storage [MWh _h]				
$vCap_{charge}$	Rated charging capacity of the TES [MWe]				
vCap _{disc harge} Rated discharging capacity of the TES [MW _e]					
vH_1 Power to charging the TES [MW _e]					
vH_2 Power discharging from TES [MW _e]					

Table 7 - Variables for LWR with Crushed Rock TES

Constraint	Description
$vP_{2p} + vH_2 = vP$	The total power output is equivalent to the share of power produced by the LWR for the generation pool plus power from the TES
$vP_{2p} + vH_1 \le vCap$	The LWR is constrained to a maximum power output
$vP_{2p} + vH_1 \ge vCap * \rho_{LWR}^{min}$	The LWR is constrained to a minimum power output
$vP \ge vCap * \rho_{Turb}^{min}$	The generator is constrained to a minimum power output
$vP \le vCap*(1+\delta^{heat})$	Total power to the grid is limited by the system capacity
$(vP_{2p} + vH_1)_t - (vP_{2p} + vH_1)_{t-1} \le vCap * \rho_{LWR}^{ramp-up}$	Changes in power output are limited by the ramp-up rate
$(vP_{2p}+vH_1)_{t-1}-(vP_{2p}+vH_1)_t\leq vCap*\rho_{LWR}^{range-down}$	Changes in power output are limited by the ramp-down rate
$vL \le vS$	The amount of energy stored [MWh] is limited by the size of the TES
$vL_t = vL_{t-1} + \alpha * vH_1 * \eta_{charge} - (vH_2 * \alpha)/\eta_{discharge} - \gamma * vL_{t-1}$	The amount of energy stored is equal to the previous time step of storage plus charge, minus discharge
$vH_1 \le \alpha * vCap_{charge}/\eta_{charge}$	The charging capacity is limited by a maximum power
$vH_1 \le (vS - vL_{t-1})/(\eta_{charge} * \alpha)$	The charging capacity is limited by the remaining storage capacity
$vH_2 \le \alpha * vCap_{discharge} * \eta_{discharge}$	The discharging capacity is limited by a maximum power
$vH_2 \le \alpha * vL_{t-1}/(\eta_{discharge})$	The discharging capacity is limited by the amount of stored energy

Objective cost functions are used to evaluate the cost-competitiveness of each formulation as demonstrated below. The fuel and variable operations and maintenance cost of the TES are assumed negligible.

Table 8 - Objective Cost Functions

Scenario	Cost Function for Nuclear Generation
Base-case w/o TES	$min[(capital + fixed \ O\&M) * vCap + (fuel + var. O\&M) * vP]$
Base-case with TES	$\min[(capital + fixed \ O\&M)_{LWR} * vCap + (fuel + var. \ O\&M) * (vP_{2p} + vH_1)]$
	$+(capital + fixed \ O\&M)_{TES} * vS + capital * (vCap_{charge} + vCap_{discharge})]$

4.4 Model Input Estimates

4.4.1 Parameter Estimates for Existing Technologies

Useful models require accurate estimates for generator operational and cost parameters. The GenX optimization used here considers investment decisions for one year. Thus, the capital costs are annualized to provide relevant comparisons between technologies with different construction and operation times. The equation below is used to calculate the future cost (Fc) of construction for a technology at the time operations begin as a function of the construction cost (I_o), interest rate (r), and construction time in years (n_c). The construction cost includes capital costs for a technology, including direct construction costs, licensing, and other one-time indirect costs incurred by the owner during construction.

$$Fc = I_o * \frac{e^{rn_c - 1}}{rn_c} \tag{27}$$

The future cost is then repaid over the operating lifetime of the technology, with profits discounted at the same discount rate. The equation below is used to calculate the annualized investment $\cos t$.

$$A = Fc * \frac{e^{rn_0}(e^r - 1)}{e^{rn_0} - 1}$$
 (28)

Detailed below are annualized costs for natural gas, coal, nuclear, nuclear with hot rock, land-based wind, utility-scale solar PV, and batteries. Overnight capital costs for natural gas, coal,

nuclear, wind, and solar technologies were taken from the 2017 NREL Annual Technology Baseline Data estimates for the year 2040 ("NREL Annual Technology Baseline Data" 2017). The capital cost for nuclear with crushed rock was estimated by adding \$100/kW, one fifth of the estimated cost for turbine hall modifications, to the overnight capital cost for nuclear generators provided by NREL. This increase in investment cost totals \$100 million for a 1 GW LWR and accounts for necessary modifications required to install crushed rock TES technology. These modifications may take the form of adding infrastructure to divert heat from the secondary loop to a steam-air heat exchanger, or simply the addition of a steam air heat exchanger to the secondary loop. The energy transferred at such an exchanger would be determined by the mass flux of air on the cold side; higher air flow would result in greater energy transfer and thus faster charging of the TES system. Battery costs were taken from Lazard's 2017 levelized cost of storage analysis ("Lazard's Levelized Cost of Storage Analysis - Version 3.0" 2017). An interest rate of 7.7% is used for all calculations.

Table 9 – Annualized Cost Parameters for Generation Technologies

Technology	Overnight Cost [\$/MWe]	Construction [yr]	Life time [yr]	Investment Cost [\$/MWe-yr]
Natural Gas	782,000	2	30	75,127
Coal	3,342,000	2	30	321,067
Nuclear	4,776,000	7	60	511,646
Nuclear with Hot Rock	4,876,000	7	60	522,359
Wind	1,202,000	1	25	117,093
Solar	808,000	1	25	78,711
Batteries	1,600,000	1	20	169,455

Crushed rock thermal energy storage capital costs were estimated for both the charging and discharging capacity in \$/MW-yr thermal and the total storage capacity in \$/MWh-yr thermal, corresponding to charging capacity costs of \$50 and \$150/kW thermal and storage capacity costs ranging from \$1-100/kWh thermal.

The table below illustrates the fixed and variable O&M costs and fuel costs which do not depend on the lifetime of the generating technology. Parameters for natural gas, coal, nuclear, wind, and solar technologies were gathered from the 2017 NREL data, and parameters for batteries

were gathered from the EIA's capital cost estimates ("NREL Annual Technology Baseline Data" 2017; "Updated Capital Cost Estimates for Utility Scale Electricity Generating Plants" 2016).

Table 10 - Cost Parameters for Generators

Technology	Variable O&M [\$/MWh]	Fixed O&M [\$/MW yr]	Fuel Costs [\$/MMBtu]	Heat Rate [MMBtu/MWh]	Emissions [tons CO2/MMBtu]
Natural Gas	7	12,000	5.33	9.92	0.0585
Coal	5	32,000	2.00	8.8	0.1053
Nuclear	2	101,000	1.06	10.46	0
Nuclear with					
Crushed Rock	2	101,000	1.06	10.46	0
Wind	0	51,000	0	0	0
Solar	0	13,000	0	0	0
Batteries	0	40,000	0	0	0

The operational parameters listed below were estimated using the 2017 NREL data and Lazard's Levelized Cost of Storage Analysis ("NREL Annual Technology Baseline Data" 2017; "Lazard's Levelized Cost of Storage Analysis - Version 3.0" 2017). The minimum load of the reactor set at 30% is used for nuclear with hot rock to reflect the flexibility provided by the crushed rock thermal energy storage.

Table 11 - Performance Parameters for Generators

Technology	Minimum Load Turbine [%]	Minimum Load Reactor [%]	Ramp Rate [%]	Charging Efficiency [%]	Discharging Efficiency [%]
Natural Gas	0	0	1		
Coal	0.4	0	1		
Nuclear	0.5	0	0.1		
Nuclear with Crushed Rock	0.5	0.3	0.1		
Wind	0	0	1		
Solar	0	0	1		
Batteries	0	0	1	0.9274	0.9274

4.4.2 Parameter Estimates for Crushed Rock Thermal Energy Storage

The technical parameters used for the crushed rock heat storage system will largely dictate the performance of the system, and thus form the basis for the experimental design. Significant parameters for the crushed rock TES system include the marginal cost of energy storage (in \$/MWh), the capital cost of charging and discharging capacity (in \$/kW), the round-trip efficiency of storing and recovering energy, and the peaking capacity provided as a percentage of the coupled reactor's rated output. In the interest of the timescale for this experiment, favorable and unfavorable performance scenarios will be considered for the crushed rock thermal energy storage system with regards to the round trip efficiency and capital cost of charging and discharging capacity.

The capital cost of charging and discharging the system reflects the costs of the pump required to circulate the air, and the heat exchangers. Turbine halls cost on the order of \$500/kW, and include turbine generators, heat exchangers, and many other components ("Power Cycles for the Generation of Electricity from a Next Generation Nuclear Plant" 2010). The cost of heat exchangers alone is then favorably estimated to be an order of magnitude reduction from the cost of a complete turbine hall, or \$50/kW, and unfavorably as \$150/kW thermal. Round trip efficiencies for similar sensible heat storage technologies coupled to LWRs was estimated by Westinghouse to be 60% (Charles Forsberg et al. 2017). This thesis bounds Westinghouse's estimate for the round trip charging efficiency with a favorable estimate of 70% and an unfavorable estimate of 50%. Peaking potentials are estimated favorably at 25%, and unfavorably at 10% of the rated capacity of the coupled LWR. These peaking values represent reasonably achievable peaking factors from turbines constructed with peaking in mind and existing turbines, respectively. The marginal capital cost for constructing a crushed rock TES is expected to distinguish crushed rock TES, at a value near \$5/kWh thermal.

4.5 Experimental Design

This thesis considers the favorable and unfavorable parameter estimates for round trip efficiencies and capital costs of charging the system as coupled into two performance scenarios for crushed rock thermal energy storage. This coupling reduces computational stress at the cost of considering all combinations of the varied parameters.

In short, the experiment uses GenX to minimize the price of electricity both with and without the use of crushed rock TES, using historic demand data and renewable resource availability from ERCOT, while varying a carbon constraint and the capital cost of constructing crushed rock TES. Historic demand data and IR resource availability has been provided by Nestor Sepulveda, a creator of the GenX model.

Each scenario considers a green field scenario with varying carbon constraints, allowing GenX to optimize the generation portfolio. The availability of LWRs coupled to crushed rock TES is also varied, considering favorable and unfavorable performance cases for crushed rock TES with capital costs of constructing the system of \$1, \$5, \$10, \$50, and \$100/kWh thermal, as well as a base case scenario without thermal energy storage. In total, one set of demand and resource data, seven carbon constraints, two crushed rock performance scenarios with five potential capital costs, and a base case without thermal energy storage results in 77 total scenarios. Capacity investment decisions under various conditions will illustrate the value of crushed rock TES. The figure below illustrates the experimental design.

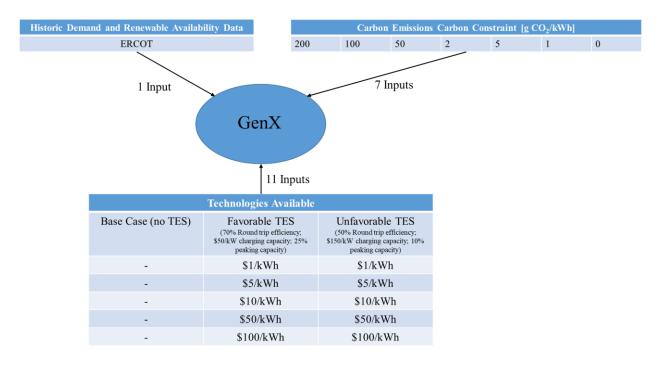


Figure 27 - Experimental Design

5. Results and Discussion

5.1 Base Case Investments

The base case scenario, without the option to invest in crushed rock TES, forms the basis for analysis. The figure below illustrates the effect of a carbon constraint on capacity investment decisions. All values for invested capacity reported in MW throughout this chapter are in MW electric. All marginal cost values for reported in \$/kWh refer to the cost per kWh of heat stored. All carbon constraints reported in g CO₂/kWh refer to grams of CO₂ emitted per kWh of electricity produced.

The data used for analysis here was taken from the independent system operator for Texas, ERCOT. As seen below, the Texas grid is a favorable environment for renewables with plentiful wind and solar availability coupled with cheap natural gas prices. Thus, ERCOT provides a conservative case for the deployment of thermal energy storage systems; if ERCOT data leads to heavy investment in thermal energy storage, then the northeast US would likely invest even more heavily in thermal energy storage technologies.

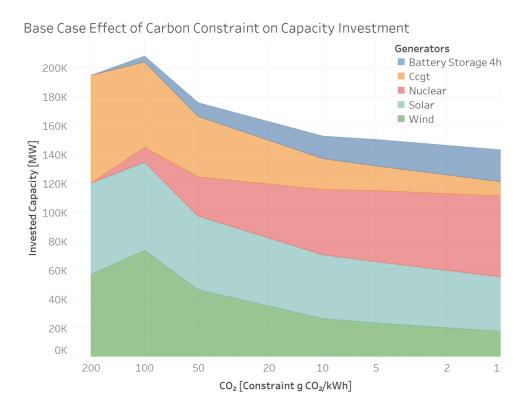


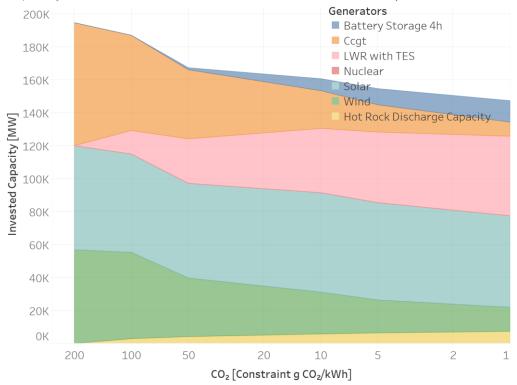
Figure 28 - Base Case Capacity Investments without TES

As shown in the above figure, investment in nuclear generation increases with an increasingly restrictive carbon constraint. The total invested capacity grows as well until a constraint set at 100 g CO₂/kWh before declining with an increasingly restrictive constraint. Investment in wind generation increases until an emission constraint of 100 g CO₂/kWh with natural gas providing electricity at times of low wind availability. Increasing the constraint beyond 100 g CO₂/kWh forces natural gas out of the system, and nuclear generation enters as a partial replacement. Wind generation decreases as nuclear replaces natural gas, which previously acted as a low cost substitute for wind at times of low wind availability. Battery storage also increases at very severe emissions constraints to balance intermittency and partly replace natural gas for peak production.

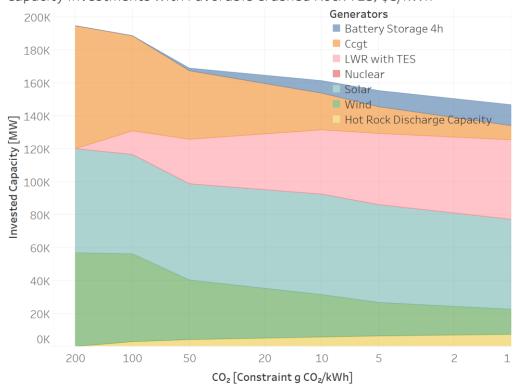
5.2 Favorable TES Results

The following figures illustrate the capacity investments resulting from favorable estimates for crushed rock TES (70% round trip efficiency; \$50/kW charging capacity; 25% peaking capacity) at marginal costs ranging from \$1 to \$100/kWh. The LWR has an additional cost of \$100/kWe for coupling to TES. Investment in electricity generation from burning coal is not shown, as investment in coal capacity was never favored. The light pink sections labeled "LWR with TES" represent the capacity of the coupled LWRs alone without peaking capacity from the TES. Peaking capacity from TES is illustrated separately as the yellow band at the bottom. As seen in the figures below, variations in investment differ insignificantly between the favorable trials, with investment in nuclear generation increasing as expected with an increasingly restrictive carbon constraint.

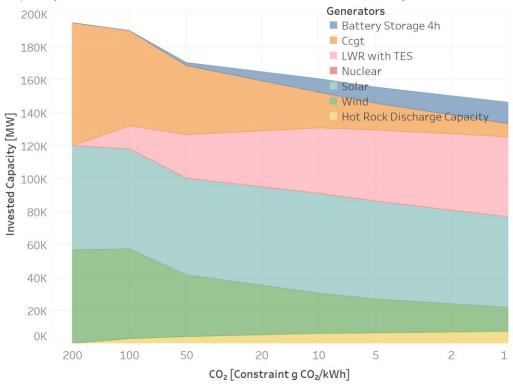
Capacity Investments with Favorable Crushed Rock TES; \$1/kWh



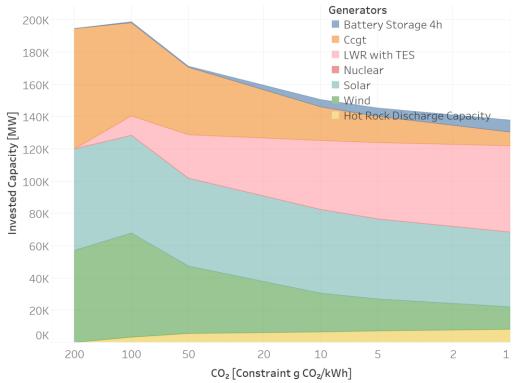
Capacity Investments with Favorable Crushed Rock TES; \$5/kWh



Capacity Investments with Favorable Crushed Rock TES; \$10/kWh



Capacity Investments with Favorable Crushed Rock TES; \$50/kWh



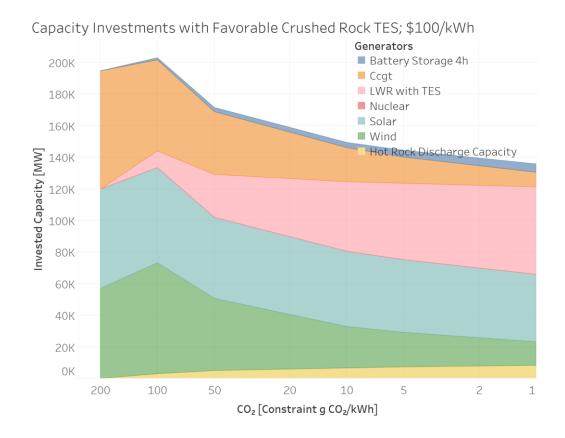


Figure 29 - Capacity Investment for Favorable Crushed Rock Parameters with Varying Marginal Cost (\$1-100/kWh heat)

Table 12 - Capacity Investments for Favorable Cases at 1 and 0 g CO₂/kWh Constraint

Capacity Investment at 1 g CO ₂ /kWhe constraint [MWe]													
TES Marginal Cost [\$/kW	h-h CCGT	ICGT	Nuclear	Wind	Solar	Battery Storage 4h	LWR with TES	TES Discharge					
Base Case (no TES)	9797	0	55942	17542	37685	21992	0	0					
1	8738	0	0	14749	55621	12844	47989	5999					
5	8603	0	0	15387	54497	12447	48299	6038					
10	8109	0	0	14673	54941	12933	48469	6059					
50	8384	0	0	13957	46481	7494	53572	6697					
100	9177	0	0	14910	42863	5303	55285	6911					

Capacity Investment at 0 g CO₂/kWhe constraint [MWe]

TES Marginal Cost [\$/kWh]	CCGT	ICGT	Nuclear	Wind	Solar	Battery Storage 4h	LWR with TES	TES Discharge
Base Case (no TES)	9797	0	55942	17542	37685	21992	0	0
1	0	0	0	7901	44388	13650	54484	6811
5	0	0	0	7967	44351	13517	54492	6812
10	0	0	0	7945	44384	13507	54501	6813
50	0	0	0	10997	28407	2413	62746	7844
100	0	0	0	8980	25900	1797	64088	8011

In summary, the model shows major differences between the base-case scenario without TES and optimal portfolios with TES available. Under favorable conditions, nuclear generation coupled to TES dominates nuclear generation without TES. Standard investment in nuclear coupled to TES also decreases battery storage, and as discussed in section 5.5, significantly decreases electricity prices.

The results reported above suggest that investment in nuclear generation coupled to crushed rock TES increases with an increasingly restrictive carbon constraint, but that the capacity share of nuclear generation and TES discharge capacity vary little with an increasing marginal cost of TES. Under favorable performance assumptions, nuclear generation coupled to TES dominates the cheaper nuclear generation without TES at any marginal cost of TES. It also seems as though more expensive TES lowers capacity investments in solar PV generation and slightly increase investment in wind, albeit well below the wind investment in the base case scenario. Also, an increasing marginal cost of TES seems counterintuitively correlated with reduced investment in battery technology. This effect may be due to the effect that expensive TES has on the average price of electricity. That is, an increase in the price of electricity due to relatively expensive TES may disproportionately harm the investment prospects for battery storage under the assumed parameters.

The formulation in GenX also allowed the system to determine both the total capacity of the TES system (MWh) and the optimal charging and discharging capacities. As the emissions constraint grows more restrictive, the ratio of crushed rock discharging capacity in MW electric to LWR capacity decreases to a value of approximately 13%. This value represents the extra peaking capacity needed to provide the coupled LWRs with the flexibility to balance supply from renewables and demand. The figure below illustrates this phenomenon for the favorable scenarios. For example, the total discharge capacity for TES in the \$10/kWh scenario amounted to between 12-14% of the total capacity of LWRs coupled to TES at a constraint of 50 g CO₂/kWh of energy produced. The figure below excludes data from a carbon constraint at 200 g CO₂/kWh because both the capacity of LWRs coupled to TES and TES discharge were found to be 0.

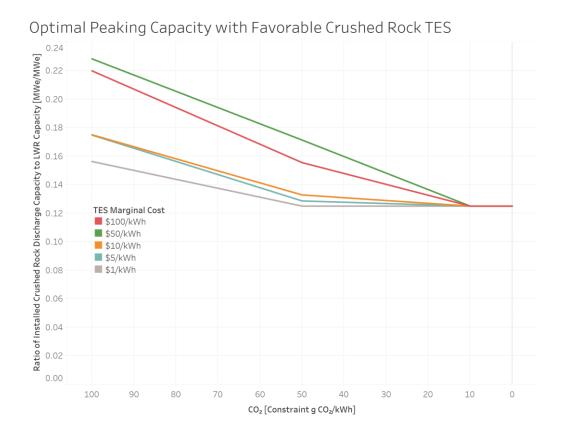
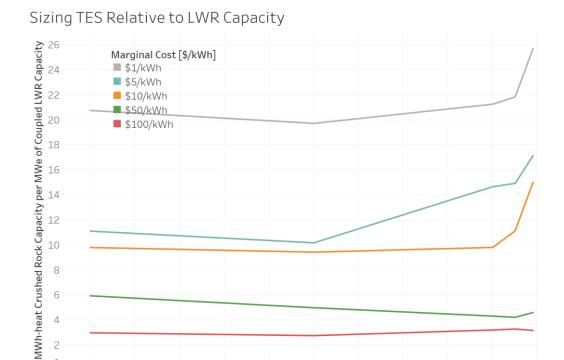


Figure 30 - Optimal Peaking Capacity for Favorable Scenarios

The following graph illustrates the optimal storage capacity under the different scenarios, with values for the favorable scenarios with marginal costs from \$5-50/kWh suggesting 6-12 MWh heat of storage capacity per MWe of coupled LWR capacity. For example, just above 10 MWhheat per MWe of installed LWR capacity would be optimal at a TES marginal cost of \$5/kWh and carbon constraint of 50 g CO₂/kWh. The sharp rise at a very restrictive carbon constraint reflects the increased demand for total TES capacity in the complete absence of natural gas.



2 0

100

90

80

70

60

Figure 31 - Sizing TES Capacity [MWh] for Favorable Scenarios Relative to Installed LWR Capacity [MWh-heat/MWe]

30

20

10

50

CO₂ [Constraint g CO₂/kWh]

The mixture of nuclear investment is interesting as well. Nuclear generation without crushed rock TES, which is \$100/kWe cheaper than LWR with TES, is never preferred to the LWR coupled to crushed rock TES under the assumed conditions. However, total investment in crushed rock TES capacity decreases as the marginal cost of the system increases. The figure below illustrates this phenomenon of decreasing investment in crushed rock TES as the marginal cost of storage increases for favorable scenarios. The graphs in Figure 29 provide the total capacity of the coupled LWRs for comparison. For example, optimal TES capacity investment amounts to approximately 300 GWh-heat coupled to 14.5 GWe of nuclear generation with a \$1/kWh TES marginal cost and 100 g CO2/kWh constraint. The exact trends between the discrete scenarios (\$1, 5, 10, 50, and 100/kWh) are uncertain, but represented here as linear relationships.

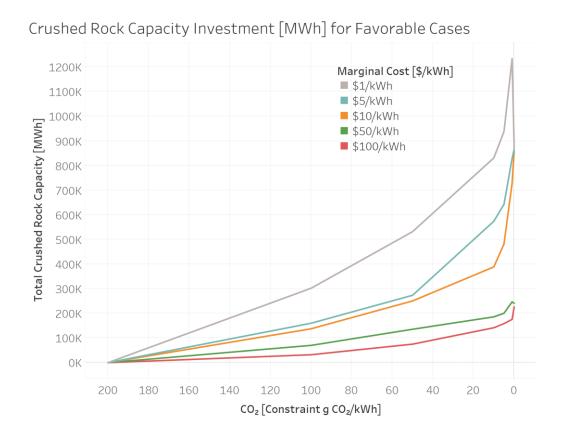
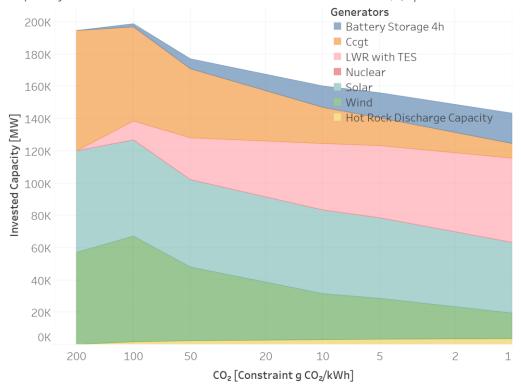


Figure 32 - Total Capacity Investments for TES [MWh-heat] for Favorable Scenarios.

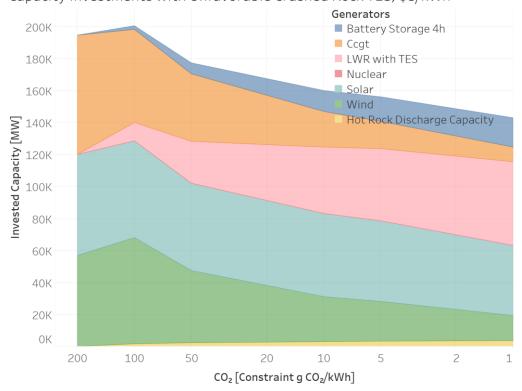
5.3 Unfavorable TES Scenario Investments

The figures below illustrate the capacity investments for unfavorable crushed rock conditions (50% round-trip efficiency; 10% peaking capacity; \$150/kW charging capacity). As with the favorable scenario, nuclear generation coupled to TES also incurs a \$100/kWe cost relative to nuclear generation without TES. Unfavorable conditions result in investments in crushed rock similar to those under favorable conditions, with cases from \$1-50/kWh resembling the favorable scenarios. Nuclear generation without crushed rock TES only becomes favorable once crushed rock TES reaches a marginal cost of \$100/kWh.

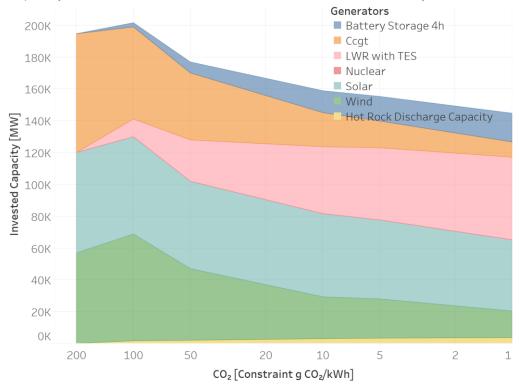
Capacity Investments with Unfavorable Crushed Rock TES; \$1/kWh



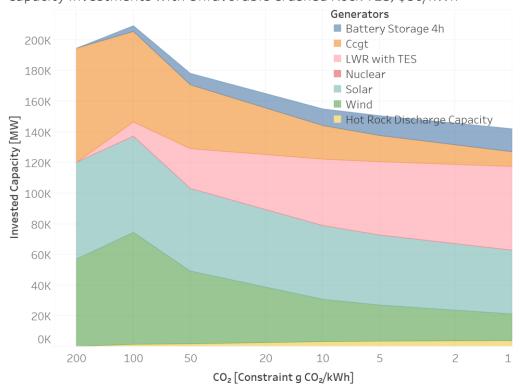
Capacity Investments with Unfavorable Crushed Rock TES; \$5/kWh







Capacity Investments with Unfavorable Crushed Rock TES; \$50/kWh



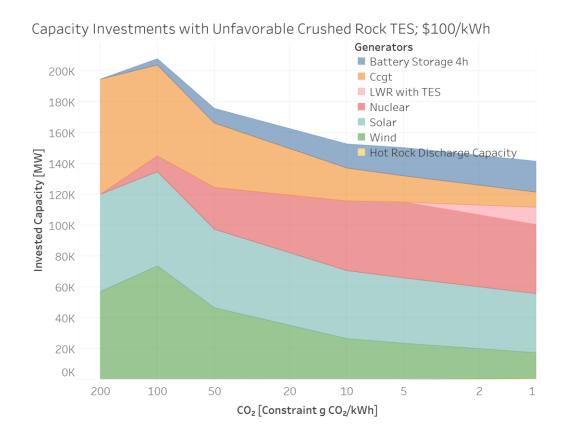


Figure 33 - Capacity Investment for Unfavorable Crushed Rock Parameters with Varying Marginal Cost (\$1-100/kWh heat)

5.4 Charging and Storage Level Samples

As expected, the crushed rock TES charges at times of low prices and discharges at times of high prices, resulting in similar curves to battery storage. It is important to note that the scenario with favorable crushed rock TES parameters, a marginal cost of \$1/kWh, and carbon constraint at 5 g CO₂/kWh charge and discharge over approximately ten hour periods. This charging period is expected to vary with different renewable availability, but proves the concept that crushed rock TES could provide at least daily energy storage. Storage levels are cumulative.

Heat to Storage and Topping for Favorable Case with 1/kWh and 5 g CO₂/kWh (43 GWe Coupled Nuclear Generation)



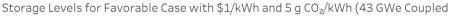


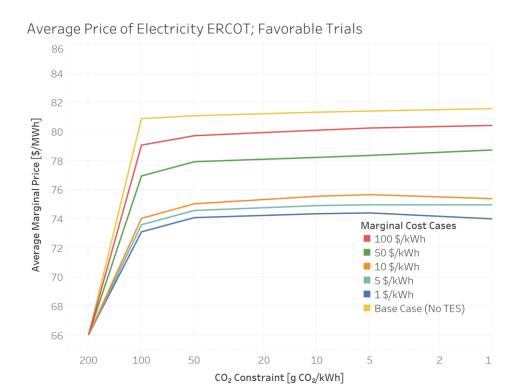


Figure 34 - Crushed Rock Charging and Discharging Profiles and Battery Comparison Over 75 Hour Window

5.5 Average Prices

The GenX model produces the shadow price, or marginal cost of electricity production, at each hour for each scenario. Average values of the marginal price for each scenario are plotted below to illustrate the effect of crushed rock TES on electricity prices. As expected, the lowest price scenario occurs with the most lenient carbon constraint, where combined-cycle natural gas plants provide peaking capacity and flexibility to energy generation. However, the average price for the base case without crushed rock TES rises to \$81-82/MWh under more restrictive emission constraints. Introducing crushed rock TES with either favorable or unfavorable parameter values results significant price reductions at restrictive emission constraints.

The option to invest in crushed rock TES with favorable parameters at \$1/kWh reduced the average marginal price of electricity from \$81/MWh to just above \$73/MWh at an emission constraint of 100 g CO₂/kWh. This corresponds to a 23% increase in the price of electricity without crushed rock TES as the carbon constraint reduces to from 200 to 100 g CO₂/kWh, but only an 11% increase in the price of electricity with crushed rock TES. Even trials with unfavorable parameter estimates reduce the price of electricity by as much as \$3/MWh at severe carbon constraints. As expected, price reductions become less significant as the marginal price of crushed rock TES increases, with cases at \$100/kWh nearly resembling the base case scenario.



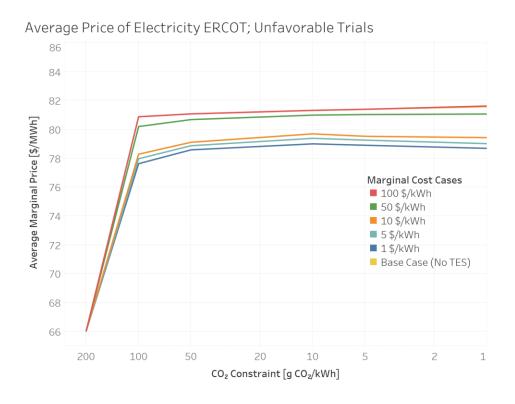
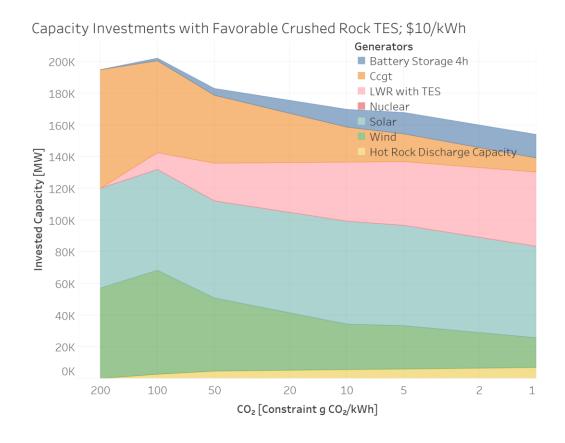


Figure 35 - Effect of Crushed Rock TES Availability on Average Electricity Prices

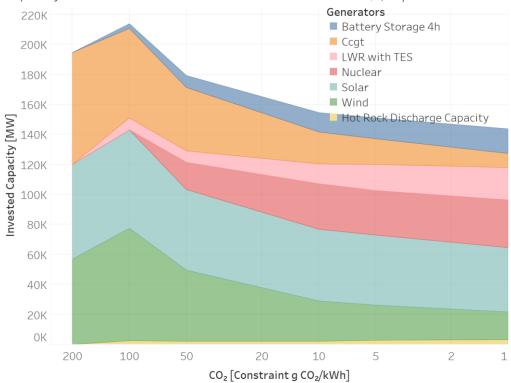
5.6 Results with \$500/kW Cost for Crushed Rock Capability

All results shown thus far carry the assumption that an LWR with the capability to couple to crushed rock TES is valued at \$100/kW overnight cost more than nuclear generation without TES. This cost amounts to \$100 million higher overnight cost for a 1 GWe reactor with crushed rock TES capability than one without. The results below illustrate the effect of increasing the difference in overnight cost to \$500/kW, or \$500 million for a 1 GWe reactor.

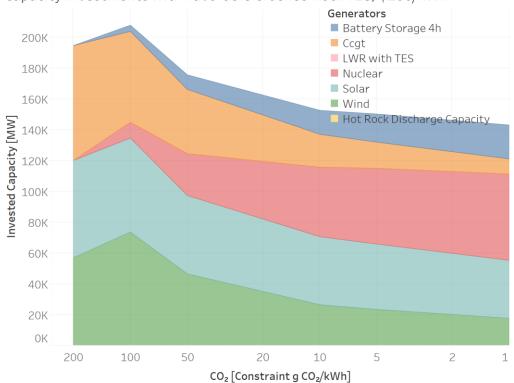
Capacity investment results are similar until a marginal cost of \$50/kWh in favorable cases, at which point a combination of LWRs with crushed rock TES and nuclear generation without TES becomes favorable. The favorable scenario with a marginal cost of \$100/kWh also shows no investment in crushed rock TES due to the high cost. Unfavorable scenarios all resemble the base case without TES, except for the scenario with a \$1/kWh marginal cost, which shows minor investment in crushed rock TES at constraints more severe than 10 g CO₂/kWh.







Capacity Investments with Favorable Crushed Rock TES; \$100/kWh



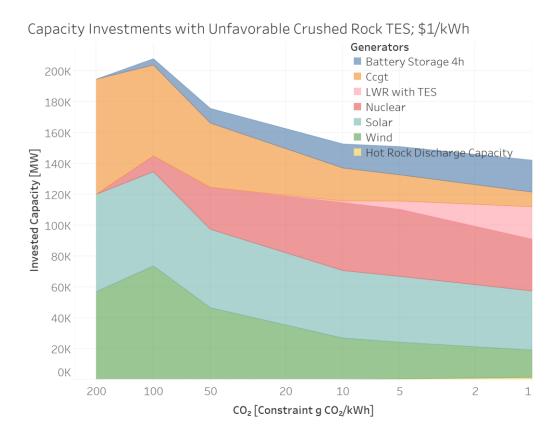
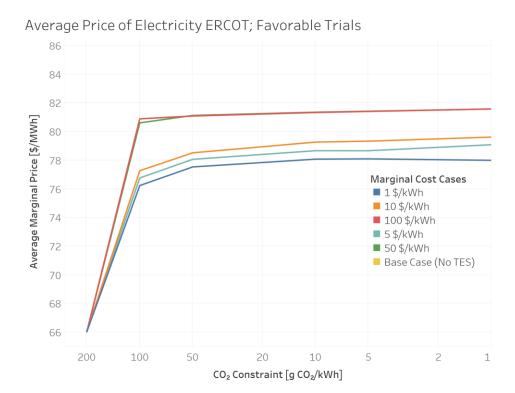


Figure 36 - Capacity Investment with High Overnight Cost for Crushed Rock Availability

Higher overnight costs for LWRs with crushed rock TES also lessened the effect of crushed rock TES on the average price of electricity as shown in the figures below. Price impacts are nearly negligible in the unfavorable cases and only drop the marginal cost of electricity approximately \$3/MWh electric in the favorable cases.



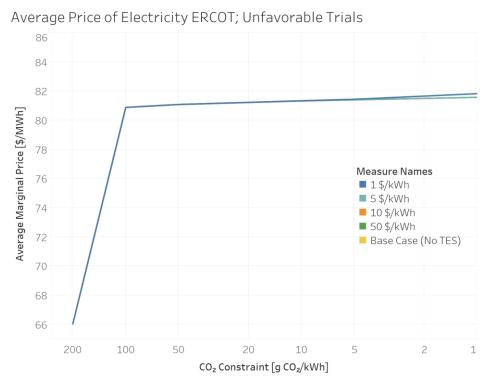


Figure 37 - Crushed Rock TES Effect on Average Prices with High Overnight Cost for Crushed Rock Availability

6. Conclusion

6.1 Policy Matters

The results illustrate that coupling crushed rock TES to nuclear generation can provide flexibility to nuclear generation, better enabling them to load follow. As a result, crushed rock TES can result in significant price reductions for generation portfolios with significant amounts of renewable energy generation and low amounts of fossil fuel burning plants. However, the data suggests that such a portfolio would not exist absent a constraint on carbon emissions. In the absence of emissions constraints, combined-cycle plants would provide the flexibility needed to balance demand at low cost (\$5.33/MMBtu natural gas), and battery technology could take advantage of energy arbitrage opportunities presented by heavy investment in renewable generation ("NREL Annual Technology Baseline Data" 2017). Thus, subsidies for renewable generation, however well intentioned they may be for limiting emissions, could result in energy portfolios comprised primarily of renewables, batteries, and natural gas plants.

6.2 Future Work

Results presented in this thesis are largely a product of assumptions. Parametric variations were used to capture some of the uncertainty in these assumptions, but further investigation is required. First, a sensitivity analysis is necessary to determine which parameters had the greatest impact in the variation between the favorable and unfavorable cases. Second, pilot plants should be used to experimentally confirm performance parameters. Complex interdependencies exist between system size, charging capacities, peaking capacity, and efficiency, all of which may be better understood with experimental testing on a large rock pile. As mentioned previously, the system can be modeled in one dimension, meaning useful results can be obtained from a relatively inexpensive test bed with a small cross section. Lumped parameters allowed for a relatively simple proof-of-concept here, but a better understanding of the relationships between parameters is important for real investment decisions.

The crushed rock TES system was also tested against a limited set of competing technologies with limited historic data. Fortunately, the formulation used implemented in GenX for this study is technology agnostic, and can broadly represent any heat storage technology that couples directly to a reactor. That is, the formulation used in this thesis can represent steam

accumulators or other sensible heat storage systems. Still, future studies should compare relative advantages of crushed rock TES over other storage technologies that interact differently on a system level such as FIRES, and with varying data sources representing regions favorable and unfavorable for renewable generation. The data set used in this study from ERCOT represents a region that is favorable to renewable energy generation and has cheap natural gas, making for a somewhat poor storage environment. The results found in this study suggest storage may be even more favorable in regions such as the Northeast United States. Different regional data could also verify system level effects found here, such as the effect of thermal energy storage coupled to nuclear and battery, wind, and solar investments. Additionally, including data for a heat market could illustrate the dual-use for crushed rock TES providing industry heat in lieu of natural gas. In summary, crushed rock TES, subject to parametric constraints, could reduce the price of electricity in a carbon constrained grid, but the relative advantage compared to other technologies is still uncertain in the context of LWRs.

As discussed in chapter 3, the temperature difference between the inlet and outlet of a TES system significantly impacts performance, both in terms of efficiencies and sizing of energy storage. Separate from the analysis here is the idea that crushed rock TES could be coupled to other reactor types, such as High-temperature Gas-cooled reactors (HTGRs) and Fluoride-salt-cooled High-temperature Reactors (FHRs). These reactors operate at significantly higher temperatures than LWRs, which suggests significant impacts on engineering parameters and costs. Different reactor designs provide a different market for TES with different competing technologies. Thus, further studies are required to evaluate the relative advantage of coupling TES to different reactor designs.

Appendix A – Engineering Analysis MATLAB Code

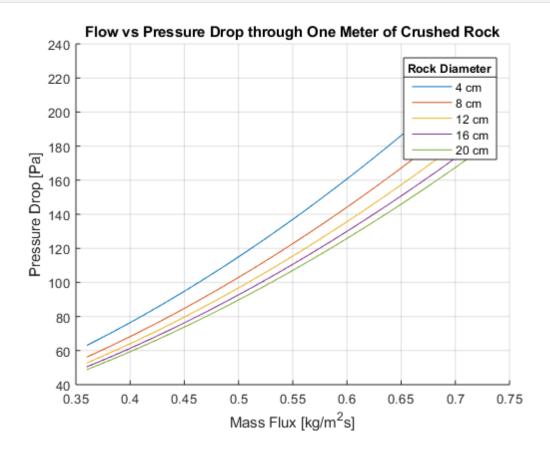
The MATLAB code used to produce the figures in chapter 3 is detailed below. Comments throughout the code explain the structure, and should provide ample guidance for clear replication.

A.1 Calculating Frictional Pressure Drop

Friction factor is determined as in Allen et al. then plotted as a function of the mass flux

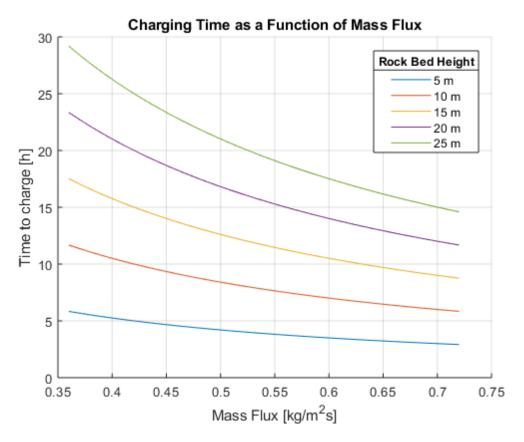
```
% Parameters
vs = linspace(1,2);
                                           % Superficial flow velocity [m/s]
alpha = 0.3;
                                           % Void fraction
rho_fluid = 1.2;
                                           % Density of air at 20C [kg/m3]
mu = 0.00001846;
                                           % Air viscosity at 20C [kg/ms]
G = vs*rho_fluid*alpha;
                                           % Mass flux [kg/m2/s]
% Write O matrices to decrease runtime
Pumping_p = zeros(100,5);
Pressure_drop = zeros(100,5);
Pressure_drop_kPa = zeros(100,5);
deltaP = zeros(1,100);
figure
hold on
grid on
% For loop calculates pressure drop for rock diameters 4, 8, 12, 16, 20 cm
for i = (1:5)
   r = i*0.02;
                                           % Radius of the rocks [m]
   DV = ((6/pi*(4/3*pi*r^3))^(1/3));
   Re = rho_fluid*vs*Dv/(mu*(1-alpha));
   f = 600./Re+12.3./(Re.^0.14);
                                           % Equation 9 from Allen et al.
   %Calculate the pressure drop through 1 meter of crushed rock
   deltaP = ((1-alpha)/(alpha^3)).*f.*(rho_fluid.*(vs.^2)/2); %[Pa]
   Pressure_drop_kPa = Pressure_drop./1000; % Pressure drop [kPa]
   % Calculate the pumping power
   Pumping_p(:,i) = deltap.*vs;
                                           %[w]
end
% Plot the pressure drop for different diameters as a function of G
plot(G,Pressure_drop)
title('Flow vs Pressure Drop through One Meter of Crushed Rock')
xlabel('Mass Flux [kg/m^{2}s]')
ylabel('Pressure Drop [Pa]')
```

```
leg1 = legend('4 cm','8 cm','12 cm','16 cm','20 cm');
title(leg1,'Rock Diameter');
```



A.2 Time to charge

```
cp_air = 1.005;
                               % Specific heat capacity of air [k]/kgK]
Tin = 500;
                               % Inlet temeorature [K]
Tout = 300;
                               % Outlet temperature [K]
                               % Specific heat capacity of granite [kJ/kgK]
c_{granite} = .790;
rho_granite = 2750;
                               % Density of granite[kg/m3]
figure
hold on
grid on
% For loop calculates times to charge at different heights
for i=[5 10 15 20 25]
                          % 'i' represents the column height here in meters
   % Temperature front speed is calculated as in equation 24
    Temperature_front_speed = ((G.*cp_air)./(rho_granite.*(1-alpha).*c_granite));
    time_to_charge = (i./(Temperature_front_speed))/3600;
    plot(G,time_to_charge)
end
ylabel('Time to charge [h]')
xlabel('Mass Flux [kg/m^{2}s]')
title('Charging Time as a Function of Mass Flux')
leg = legend('5 m', '10 m', '15 m', '20 m', '25 m');
title(leg,'Rock Bed Height');
```



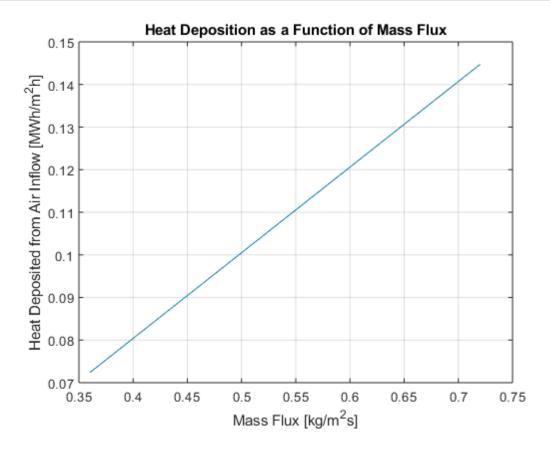
A.3 Heat Deposited from Air as a Function of mass flux

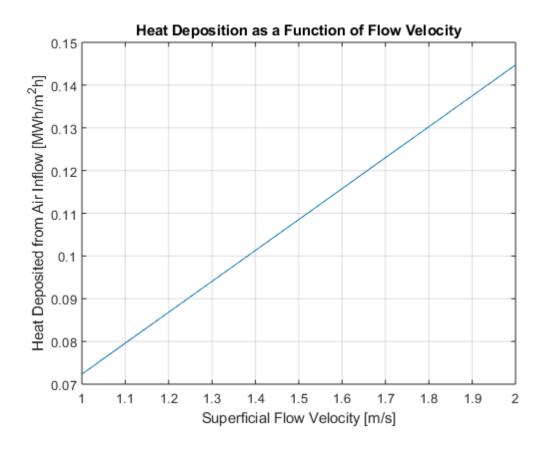
Calculate the heat deposited [MWh-heat/m2h]

```
E_deposited = cp_air*G*(Tin-Tout)/1000;

% Plot energy deposited as a function of mass flux figure  
plot(G,E_deposited)  
grid on  
xlabel('Mass Flux [kg/m^{2}s]')  
ylabel('Heat Deposited from Air Inflow [Mwh/m^{2}h]')  
title('Heat Deposition as a Function of Mass Flux')

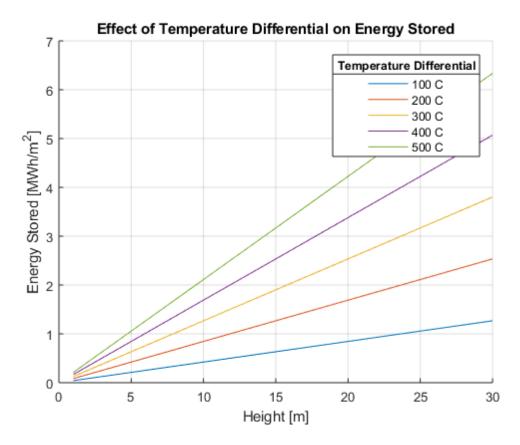
% Plot energy deposited as a function of flow velocity figure  
plot(vs,E_deposited)  
grid on  
xlabel('superficial Flow Velocity [m/s]')  
ylabel('Heat Deposited from Air Inflow [Mwh/m^{2}h]')  
title('Heat Deposition as a Function of Flow Velocity')
```





A.4 Energy Stored at Varying Temperatures

```
figure
hold on
grid on
height = linspace(1,30);
% For loop calculates energy stored with various temperature differences
for deltaT = [100 200 300 400 500]
    % Energy stored in a column is calculated as the mass of granite
    % multiplied by the specific heat capacity temperature difference
    E_column = (2.77777e-7)*(1-alpha)*rho_granite*c_granite*height*(deltaT);
    plot(height, E_column);
end
title('Effect of Temperature Differential on Energy Stored')
ylabel('Energy Stored [MWh/m^{2}]')
xlabel('Height [m]')
leg2 = legend('100 c', '200 c', '300 c', '400 c', '500 c');
title(leg2,'Temperature Differential')
```

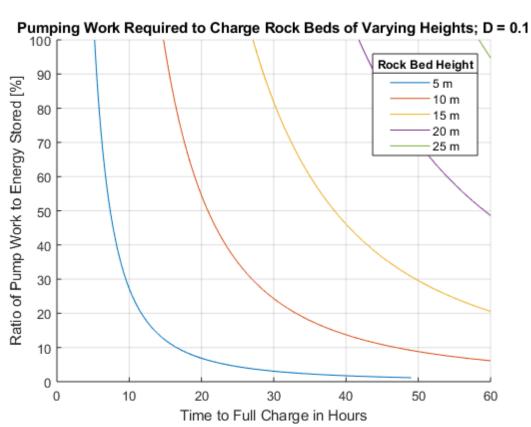


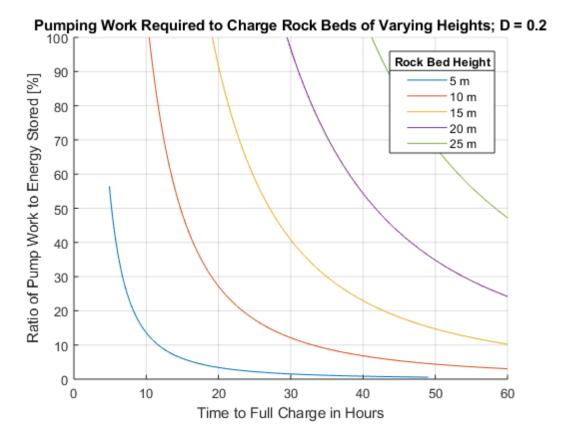
A.5 Calculating Pumping Power as in Barton

This code plots the ratio of pump work to energy stored as a function of the time to fully charge a system for rock piles of varying height. Important parameters to consider are the heat conversion efficiency, temperature difference, and rock diameter

```
% Parameters
for d=[0.1 0.2]
% Diameter of pebbles [m]
                      % Void fraction
alpha = 0.3;
alpha_i = (1-alpha);
mu_a = 0.854;
rho_a = 0.854;
Ca = 1009; %[J/(kgK)]
c_granite = 790; % Specific heat capacity of granite [kJ/kgK]
rho_granite = 27500; % Density of granite
                                                         [kg/m3]
heat_conversion_efficiency = 0.5; % Unitless
G = rho_a*v_h; % Mass flux [kg/(m2s)]
% Calculate temperature speed as before
Temperature_front_speed = ((G.*Ca)./(rho_granite.*alpha_i*c_granite));
figure
hold on
% For loop calculates data for various rock bed heights
for i = 1:5
    H(i) = 5*i; \% Height [m]
    % Calculate Delta P - Equation 18 from Barton
=(150*mu_a*(alpha_i^2).*v_h)/((alpha^3)*(d^2))+(1.755*alpha_i*rho_a.*v_h.^2)/(d*alpha^3);
    Delta_P = P_term.*H(i); % Pressure drop [Pa]
   % Calculate time to charge
    time_to_charge = (H(i)./(Temperature_front_speed)); % charging time [s]
   time_hours(:,i) = time_to_charge/3600;
   %Calculate pumping energy
    E_pump = time_to_charge.*Delta_P.*v_h;  % Pumping energy required [J/m2]
    % Compare to heat from airstream
    E_air = Delta_T*G*Ca.*time_to_charge*heat_conversion_efficiency;
    % Calculate Pump Work Ratio
    Pump_work_ratio = 200.*E_pump./E_air; %multiplied by 2 to account for discharge
    percent_power_used(:,i) = Pump_work_ratio;
end
```

```
plot(time_hours, percent_power_used)
grid on
ylabel('Ratio of Pump Work to Energy Stored [%]');
ylim([0,100]);
xlabel('Time to Full Charge in Hours');
xlim([0,60]);
basetitle = 'Pumping Work Required to Charge Rock Beds of Varying Heights; D = ';
title([basetitle,num2str(d)]);
leg = legend('5 m','10 m','15 m','20 m','25 m');
title(leg,'Rock Bed Height');
end
```





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